



# The Simulation and Subseasonal Forecasting of Hydrological Variables

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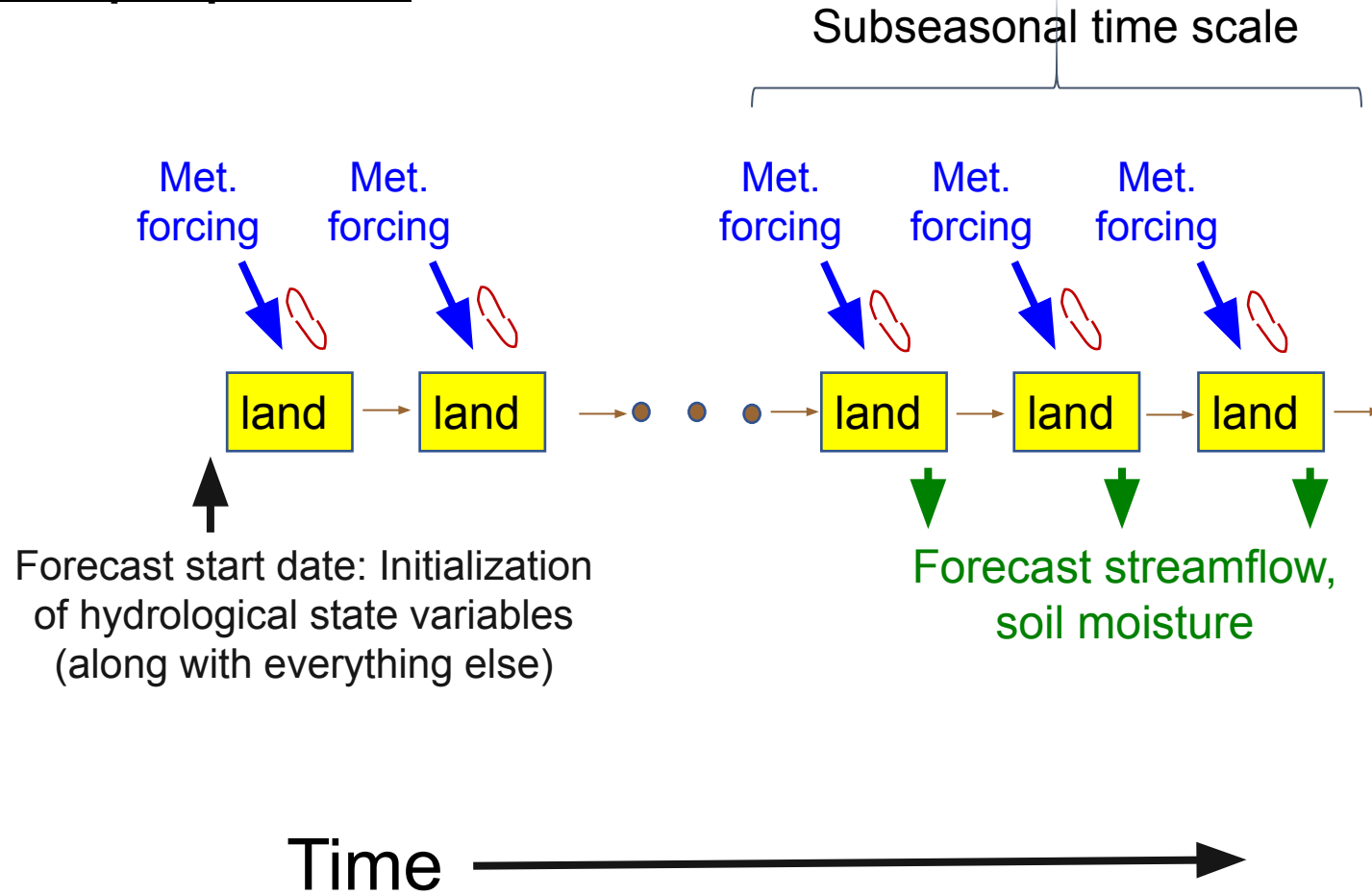
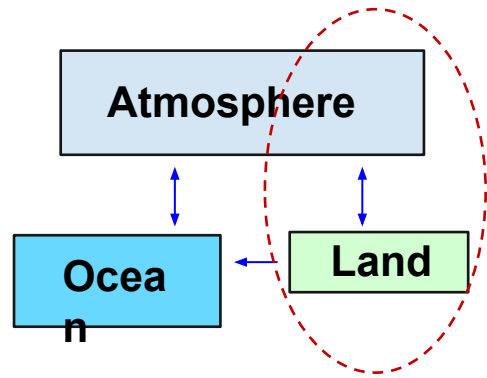
<sup>3</sup>Also with Science Systems and Applications, Inc.



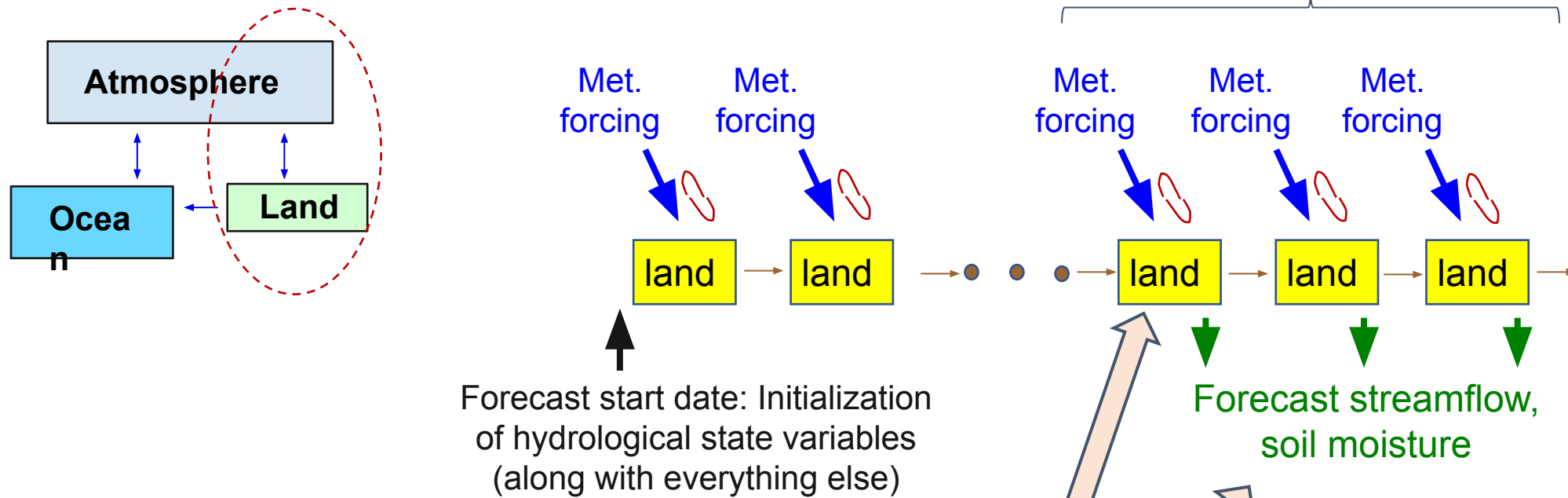
## **Hydrological variables: Important to predict at subseasonal time scales.**

- Soil moisture anomalies (e.g., agricultural planning)
- Streamflow anomalies (e.g., water resources planning, flooding preparedness)

# From a hydrological forecast perspective...



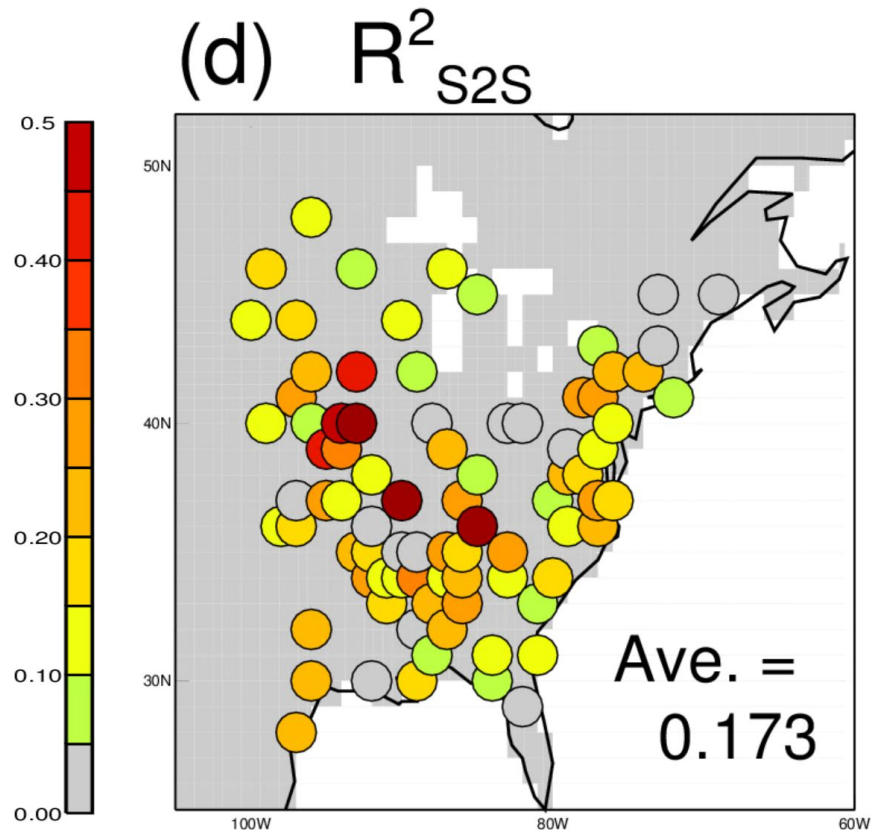
## From a hydrological forecast perspective...



To what extent does a land model's design, all by itself, affect hydrological forecast skill (in terms of anomaly prediction, not just absolute magnitudes), regardless of how good the meteorological forecasts are?

*That is, can we improve hydrological forecast skill by optimizing the land model itself?*

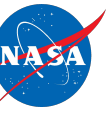
## Current level of skill for the GMAO S2S forecast system: Forecast soil moistures vs. in situ observations



Soil moisture forecast skill (anomaly  $R^2$ ) at 11-20 day lead, as determined against in-situ soil moisture measurements. Hindcast period considered: May-September of 1999-2020.

(from <https://doi.org/10.1175/JHM-D-22-0050.1>)

*How do we go  
about improving  
on this?*



## **Step 1 of Approach:**

Examine problem with a “bare bones” representation of a land surface model.

# Bare-bones representation: the “WBM”, based on water balance equation

Soil profile water  
holding capacity

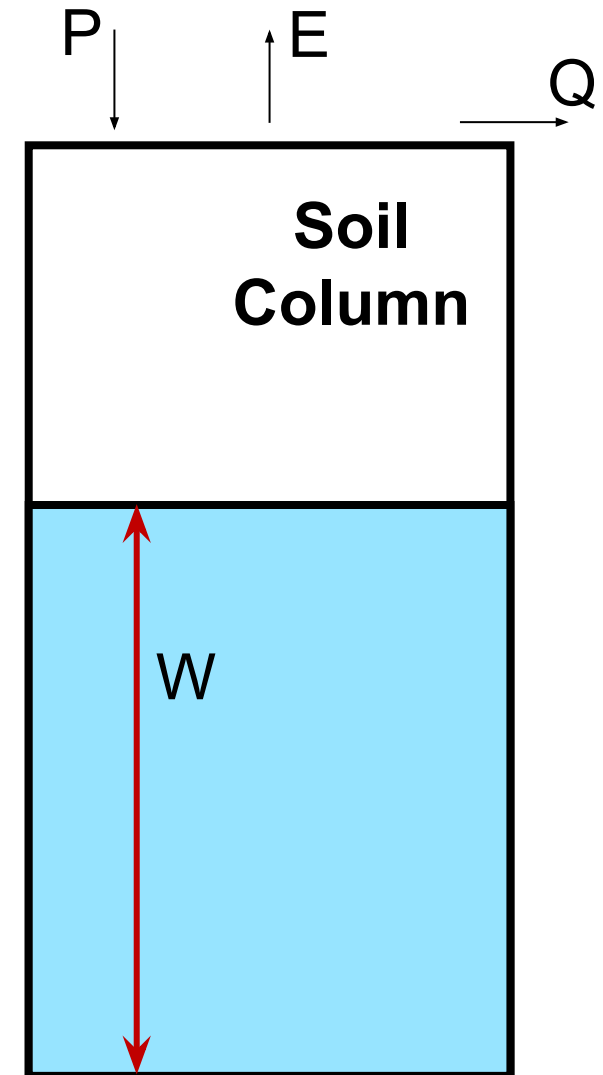
Precipitation

Evapotranspiration

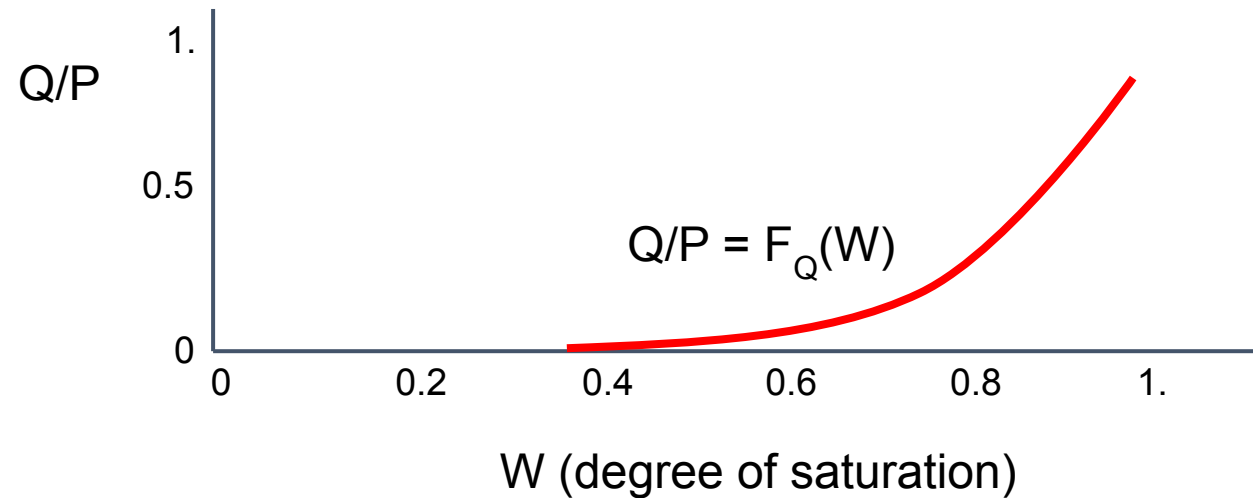
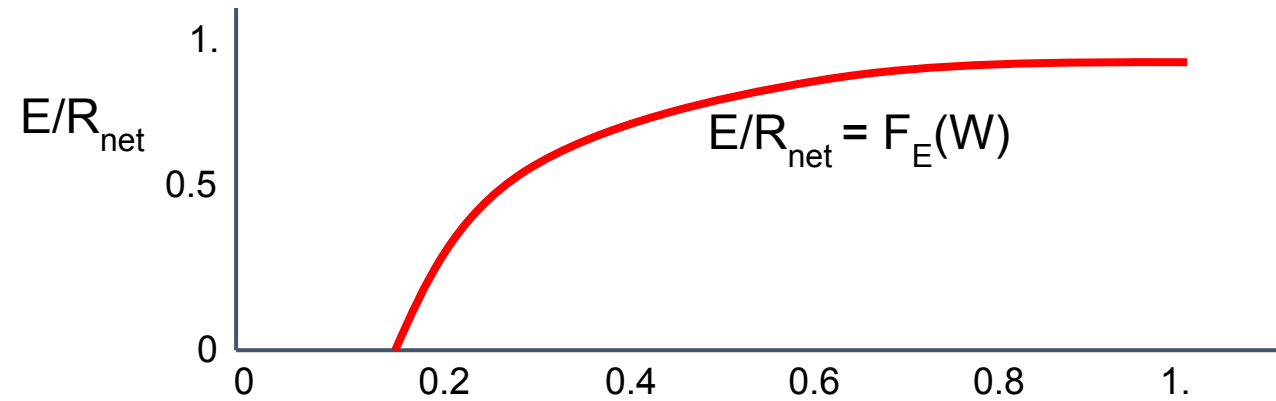
$$C W_{n+1} = C W_n + P_n - E_n - Q_n,$$

Total runoff

Soil moisture at start of day n (degree of saturation)



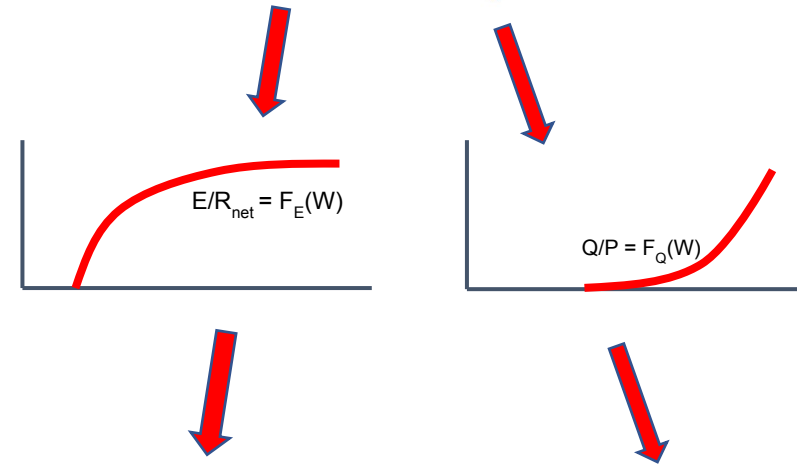
We can impose simple relationships between  $W$  and both  $E$  and  $Q$ :





□ Replace

$$C W_{n+1} = C W_n + P_n - E_n - Q_n$$

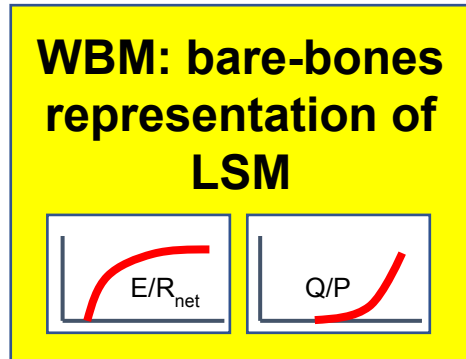
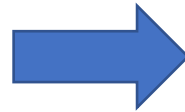


with

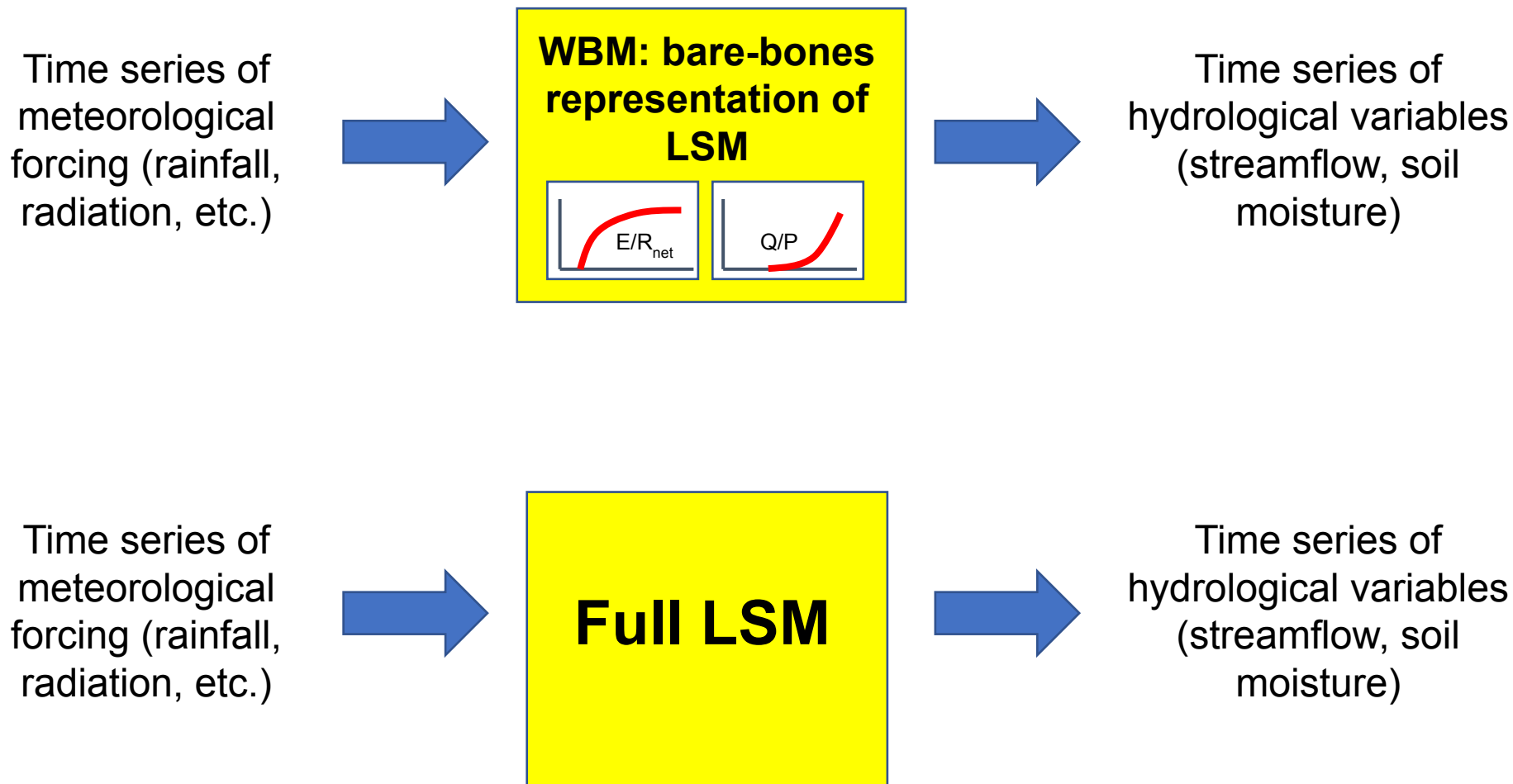
$$C W_{n+1} = C W_n + P_n - F_E(W_n) R_{\text{net-n}} - F_Q(W_n) P_n$$

This, in a nutshell, is the bare-bones representation.

Time series of meteorological forcing (rainfall, radiation, etc.)



Time series of hydrological variables (streamflow, soil moisture)



*Can we calibrate the WBM curves so that this...*

Time series of meteorological forcing (rainfall, radiation, etc.)



**WBM: bare-bones representation of LSM**

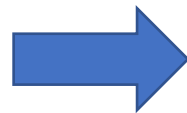


Time series of hydrological variables (streamflow, soil moisture)



*...looks like this?*

Time series of meteorological forcing (rainfall, radiation, etc.)



**Full LSM**

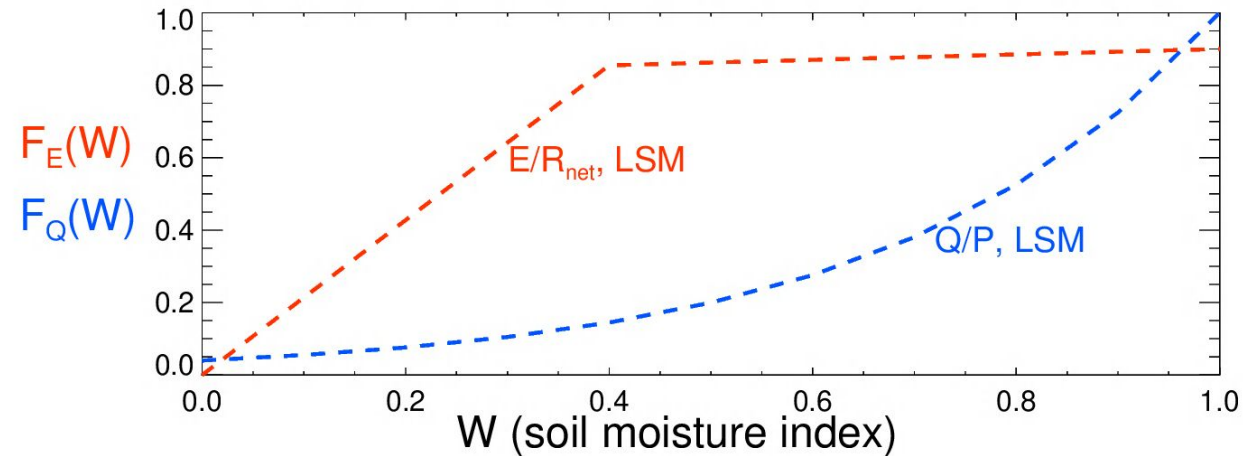


Time series of hydrological variables (streamflow, soil moisture)



# YES!

-- Calibrate curves to the behavior of a full LSM (the Catchment LSM, part of the MERRA-2 reanalysis) using data from 1980-1998.



-- Run the bare-bones model over 1999-2020

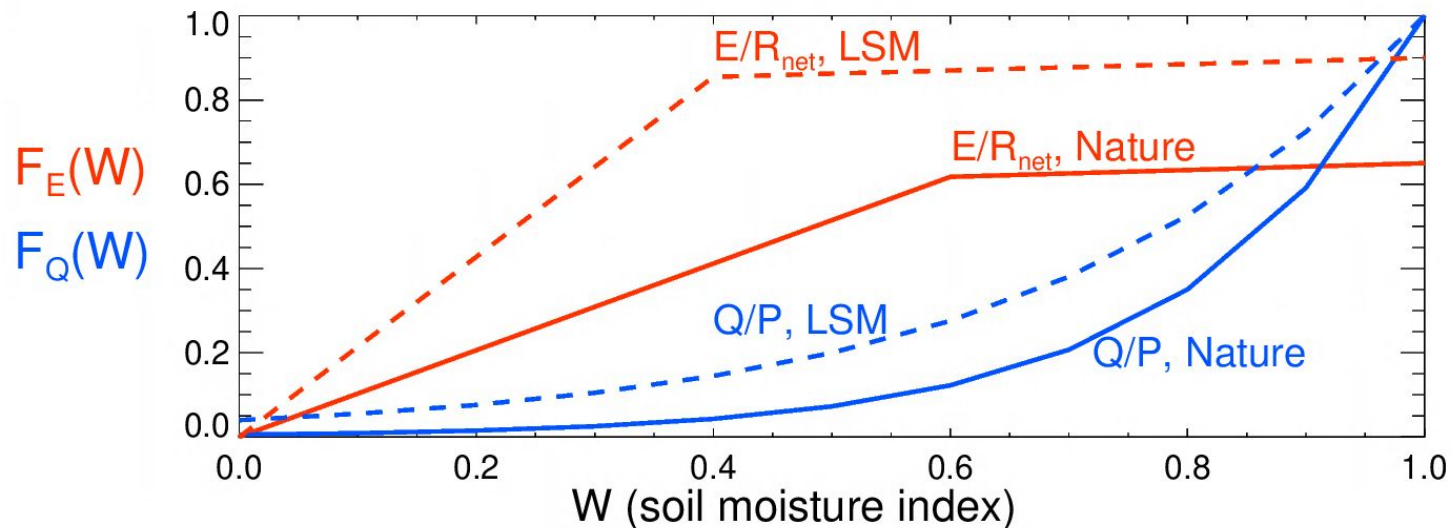
-- Compare the simulated hydrology to that of the full Catchment LSM, as produced in MERRA-2 during that latter period

☐ Nice agreement!

(not shown here due to time constraints, but see [doi:10.1175/JHM-D-22-0050.1](https://doi.org/10.1175/JHM-D-22-0050.1))

But – are the calibrated curves optimal?

Recalibrate curves during the 1980-1998 period using observed streamflow as the calibration target □ get a different set of curves.

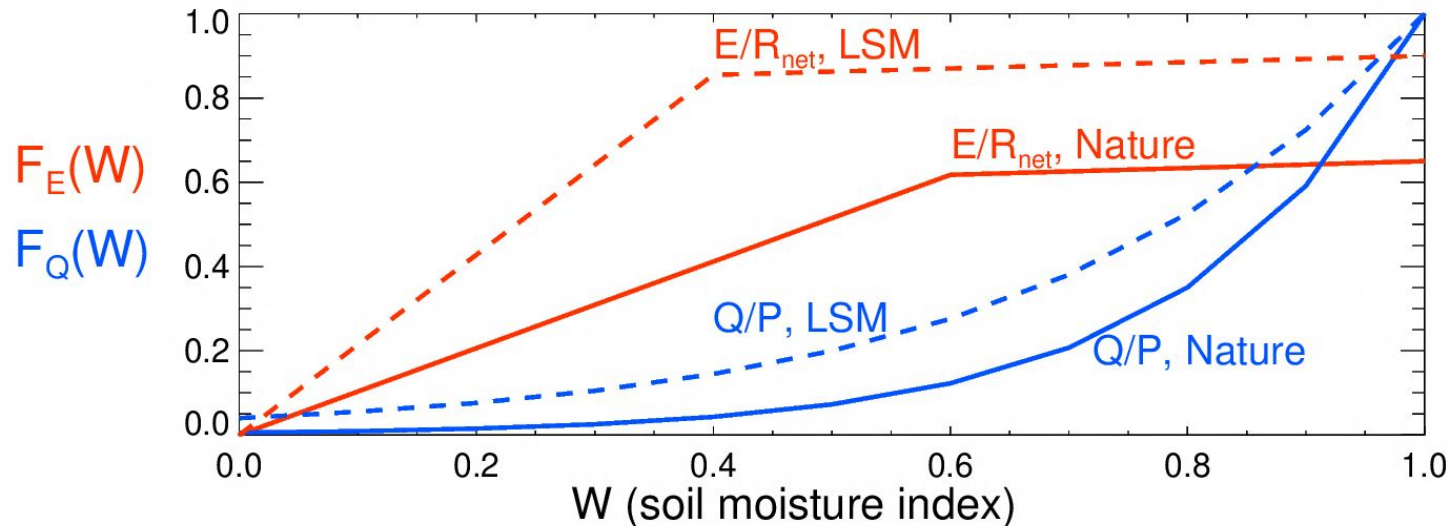


But – are the calibrated curves optimal?

Recalibrate curves  
streamflow as the c

A technical detail (just for completeness): it's not so much that the solid curves lie below the dashed curves that's important...

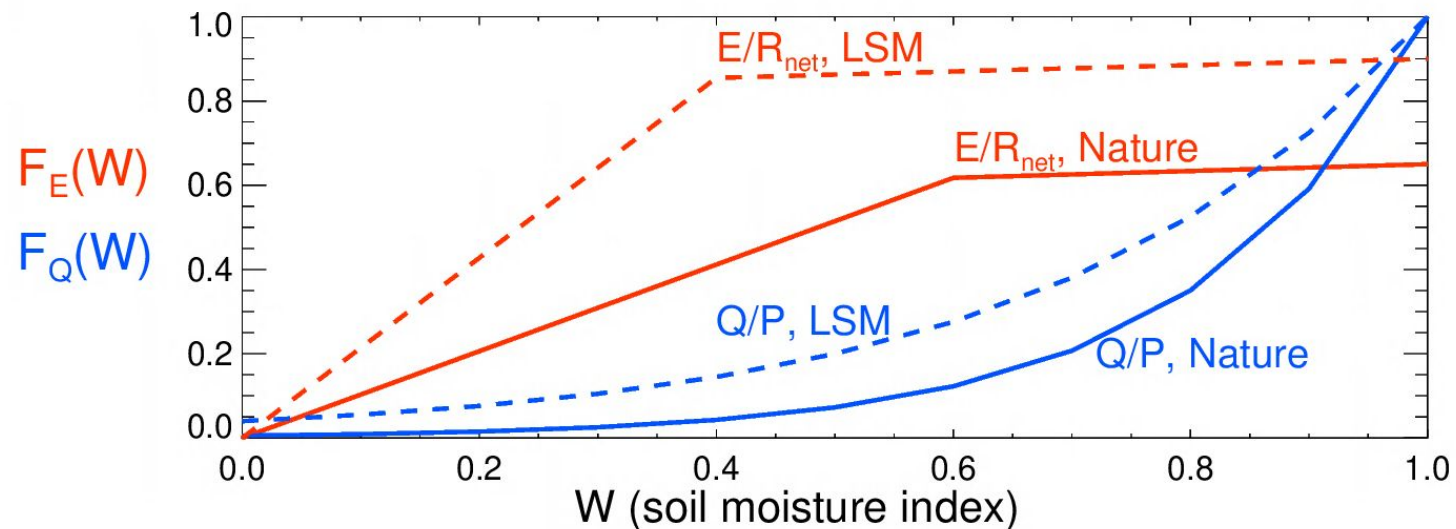
erved  
curves.



... it's that the solid curves are closer together than the dashed curves.

But – are the calibrated curves optimal?

Recalibrate curves during the 1980-1998 period using observed streamflow as the calibration target □ get a different set of curves.

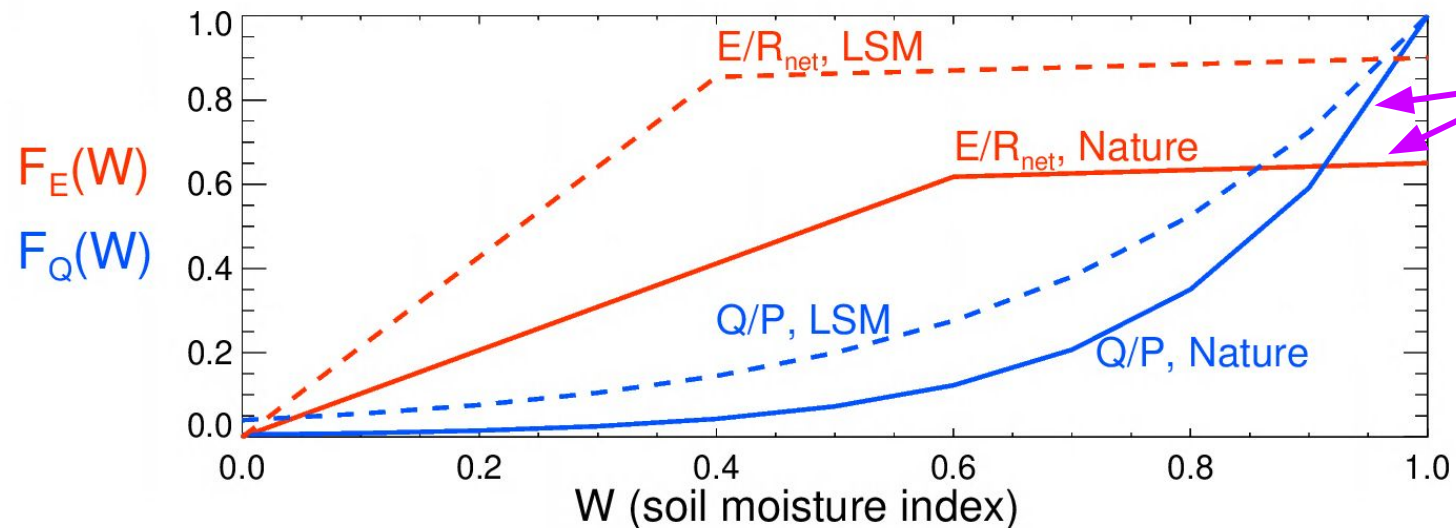


When both sets of curves are used in the WBM, and the WBM is driven with forcing in an independent time period, the “Nature” curves continue to agree with observations best.



But – are the calibrated curves optimal?

Recalibrate curves during the 1980-1998 period using observed streamflow as the calibration target □ get a different set of curves.



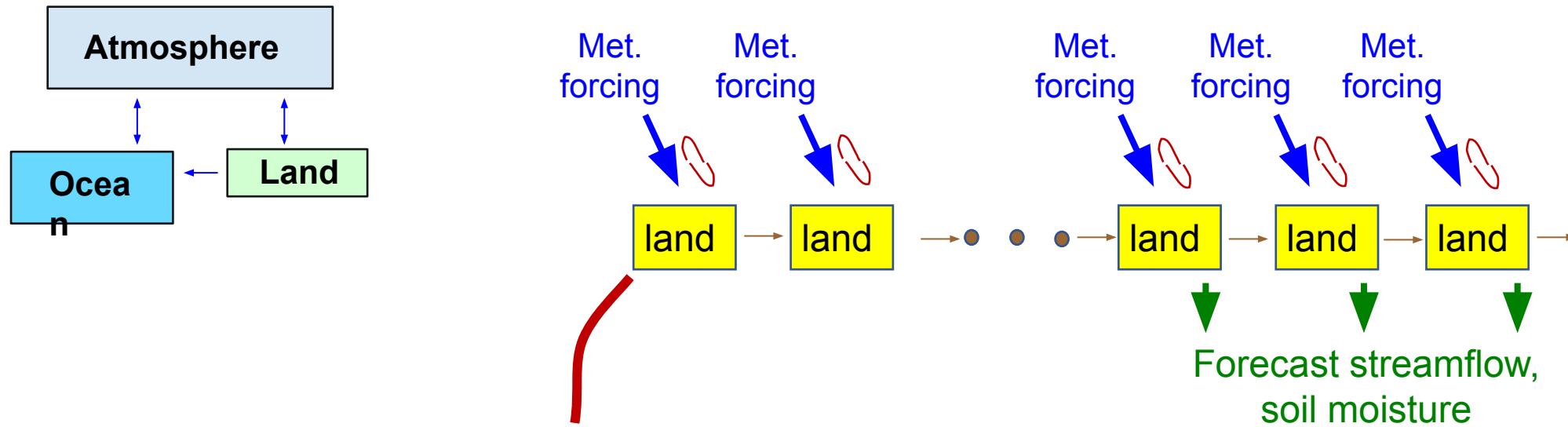
*The “Nature” curves will thus serve as our development target when improving the land surface model.*



## **Step 2 of Approach:**

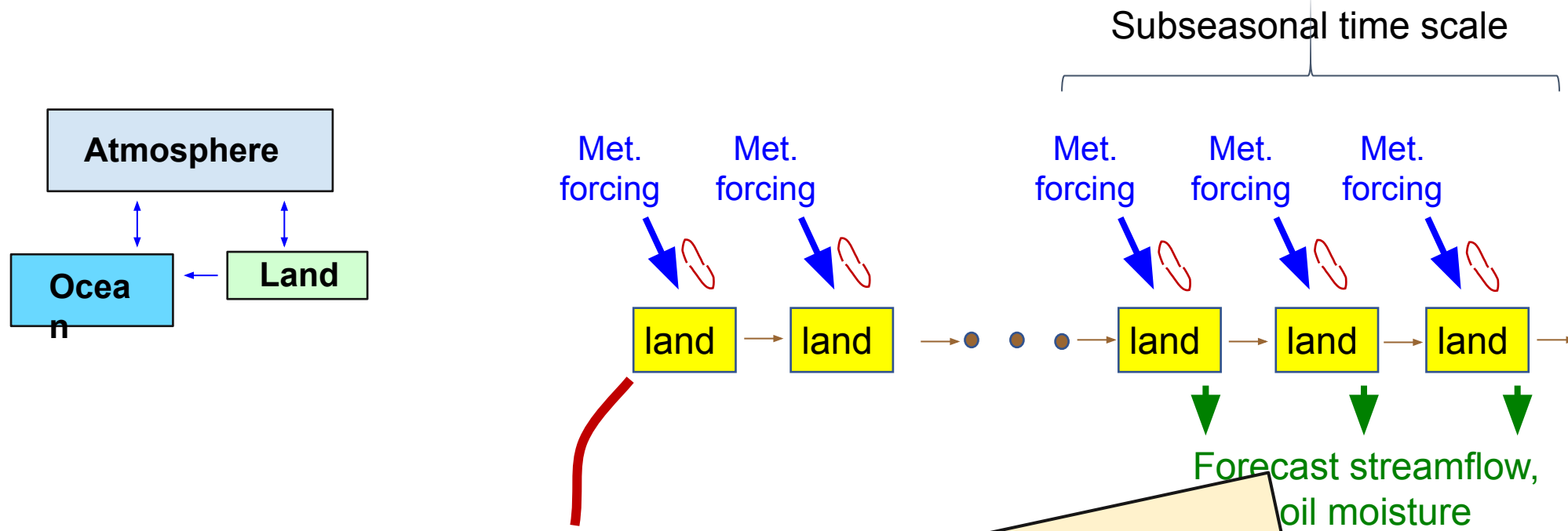
Examine the prediction problem with actual changes to the S2S system's land surface model.

## Land model impacts could be studied online...



In a series of hindcast experiments, modify the land model and see if you get better hydrological predictions

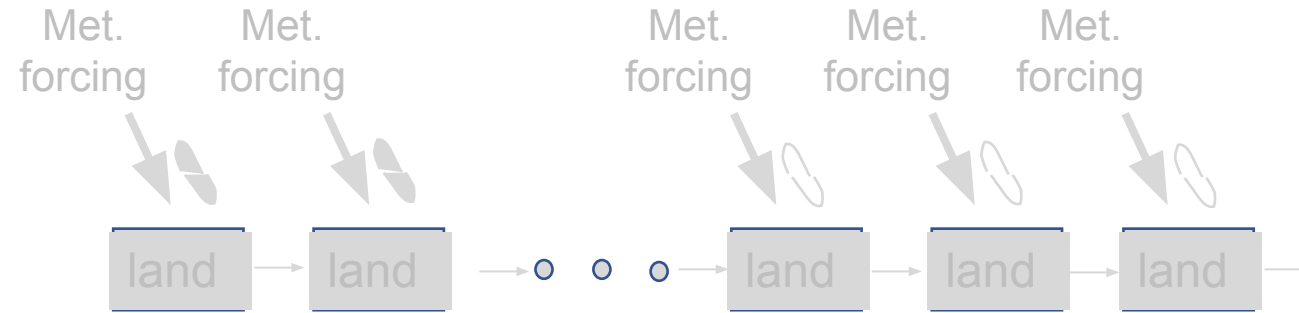
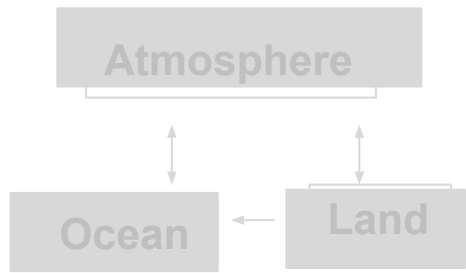
# Land model impacts could be studied online...



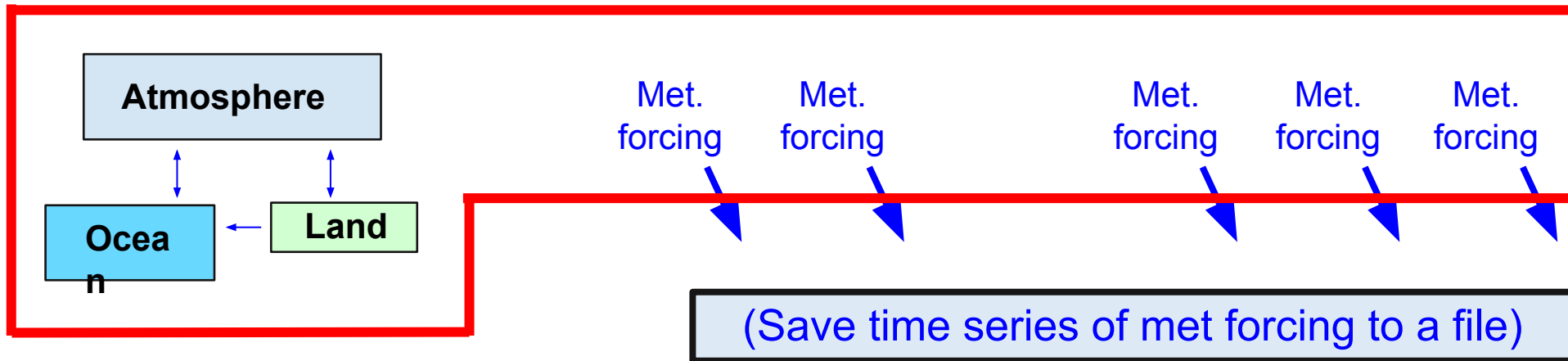
In a series of hindcast experiments modify the land model and see if you get better hydrological predictions

No – overwhelmingly expensive!

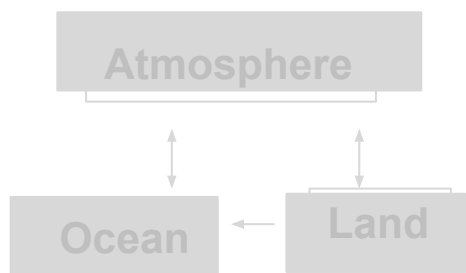
## Land model impacts can also be studied offline



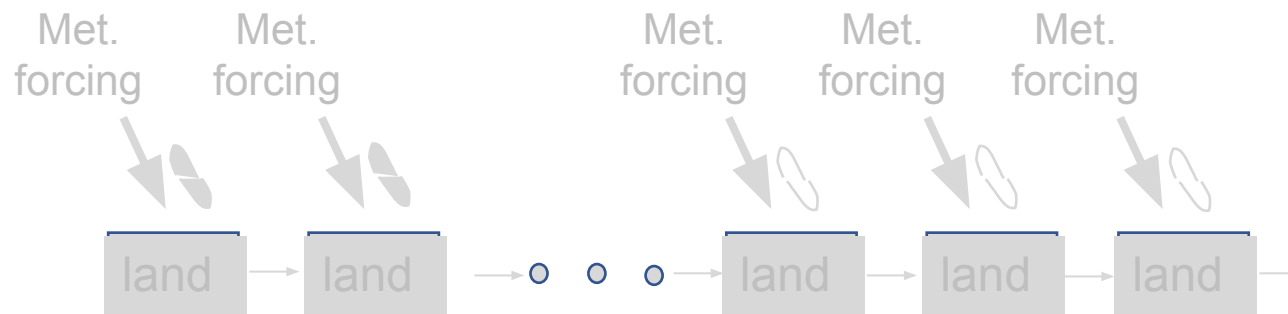
Run the full S2S set of hindcasts once, ahead of time!



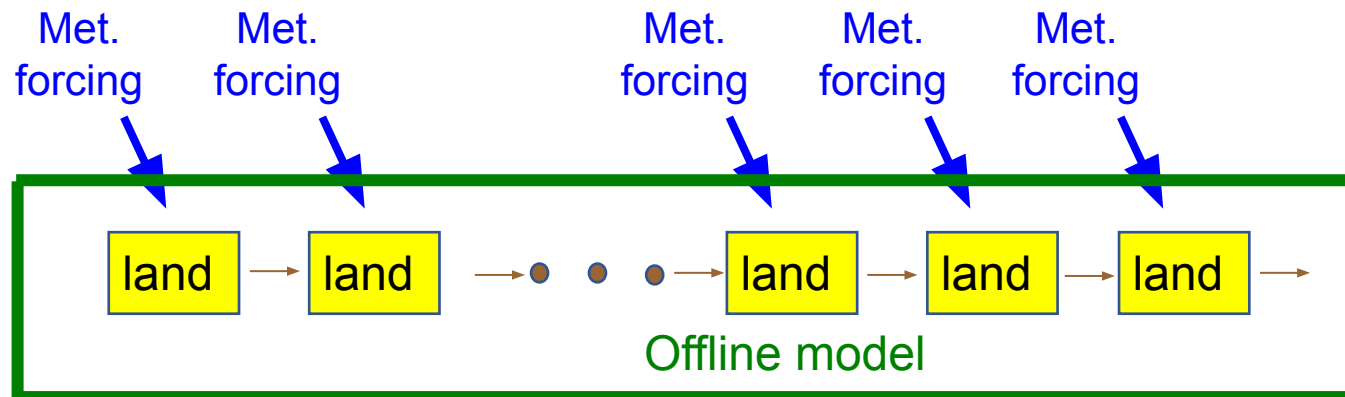
## Land model impacts can also be studied offline



Subseasonal time scale

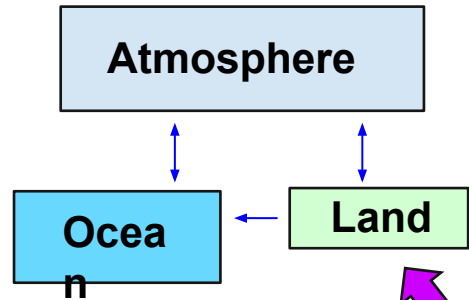


(Saved time series of met forcing, bias corrected)



Modify land model in different forecast experiments; evaluate impact on soil moisture forecast skill

# Land model impacts can also be studied offline



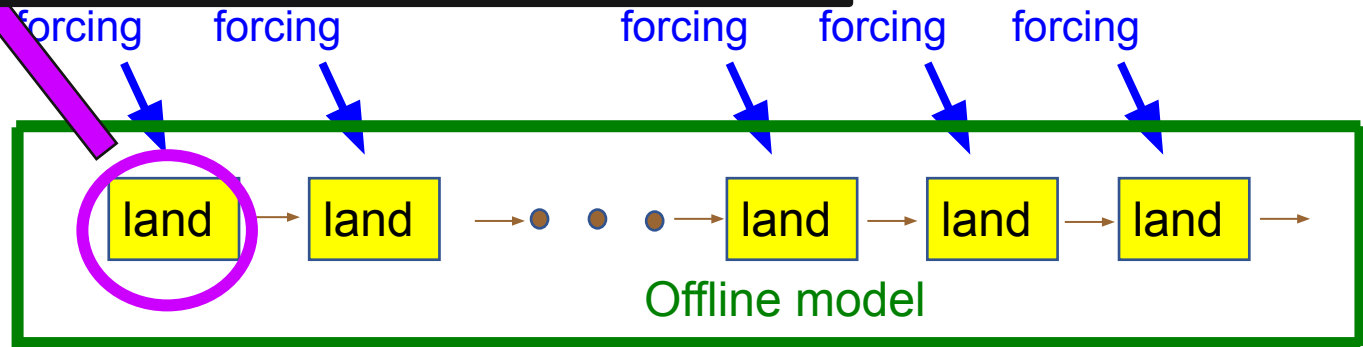
Subseasonal time scale



Eventually, put the optimized land model here for further testing with full S2S system. (A system that includes full feedbacks with the atmosphere...)

file, bias corrected)

Modify land model in different forecast experiments; evaluate impact on soil moisture forecast skill





We use the offline testing environment to improve our land model for hydrological forecasts. (Note – even with imposed bias corrections to the forcing, we will still be studying fair forecasts.)

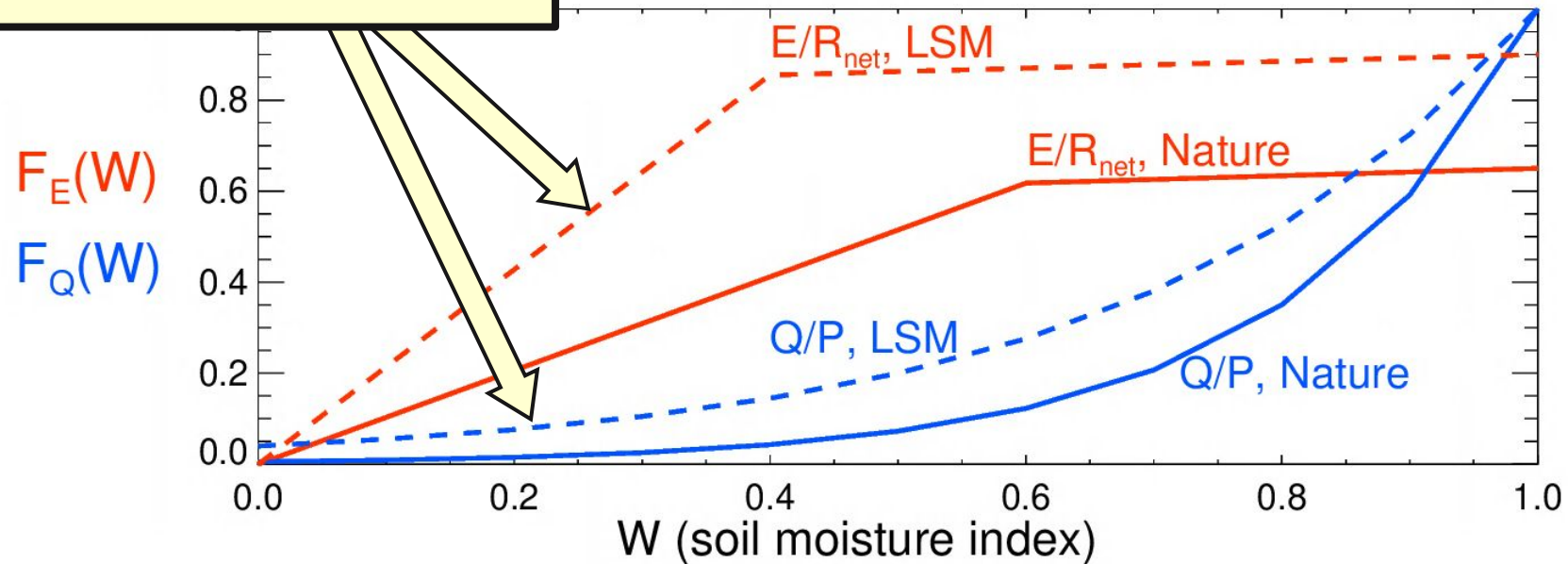
BUT, do we know how to improve the land model?

*Yes! From the “bare bones” analysis!*



That is, make the curves for the model look more like “Nature’s curves”

relationships between land model’s soil moisture variable and runoff efficiency  $[F_E(W)]$  and runoff efficiency  $[F_Q(W)]$ :



<https://doi.org/10.1175/JHM-D-22-0050.1>



## **Offline “control” forecast experiment**

Initializations: June 1, July 1, August 1 of 2001-2020, as taken from a long-term offline simulation forced with reanalysis forcing

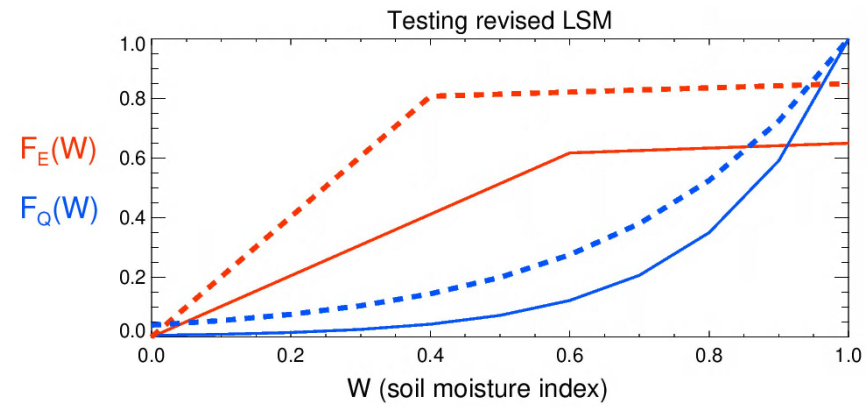
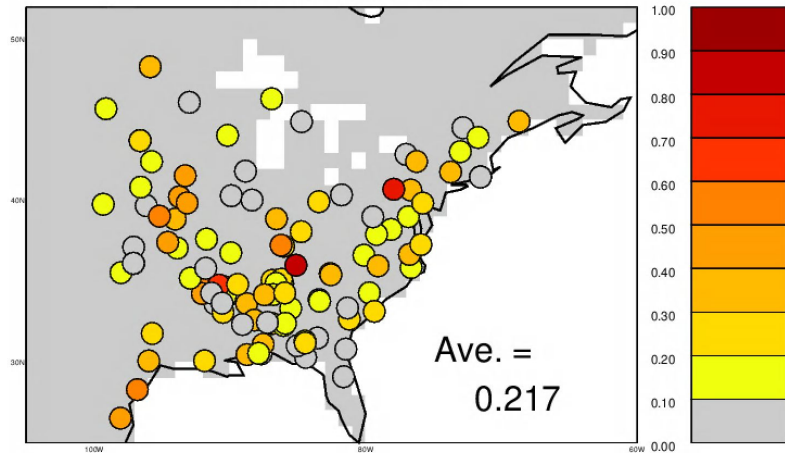
All met forcing was derived from full GMAO S2S system’s set of hindcasts, bias corrected to MERRA-2 climatologies determined during an independent period

Variable examined and compared to in-situ observations: root zone soil moisture

Lead considered in all analyses below: Days 11-20 of forecast

Thanks to Yuna Lim for all forecast production work!

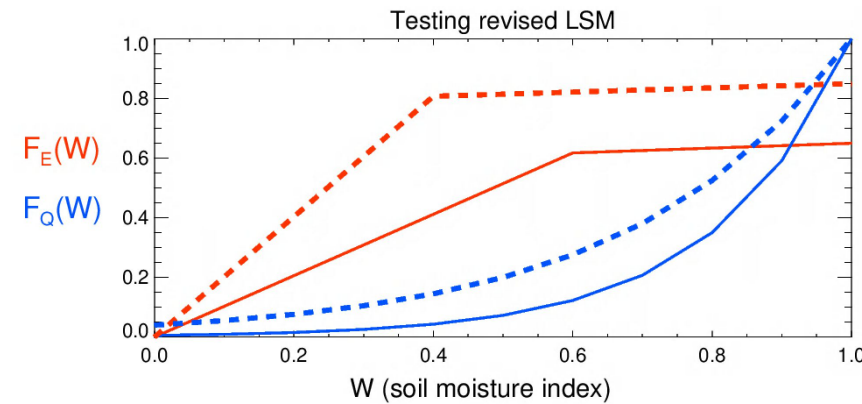
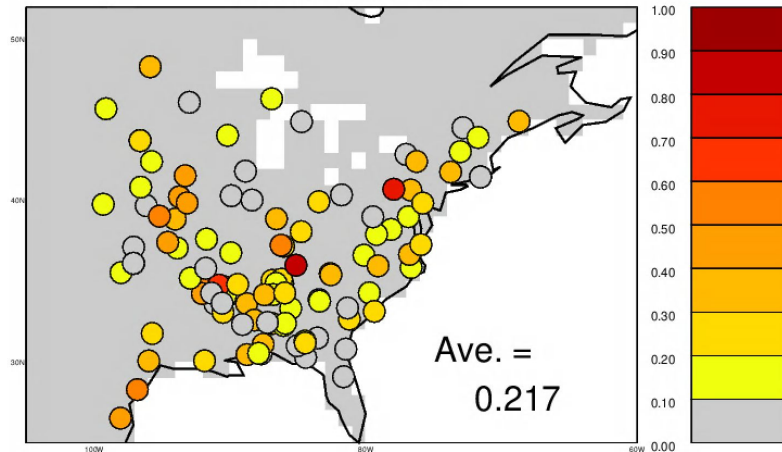
## Offline forecast skill for soil moisture ( $R^2$ )



Dashed lines: inferred model curves

Solid lines: inferred Nature curves

## Offline forecast skill for soil moisture ( $R^2$ )



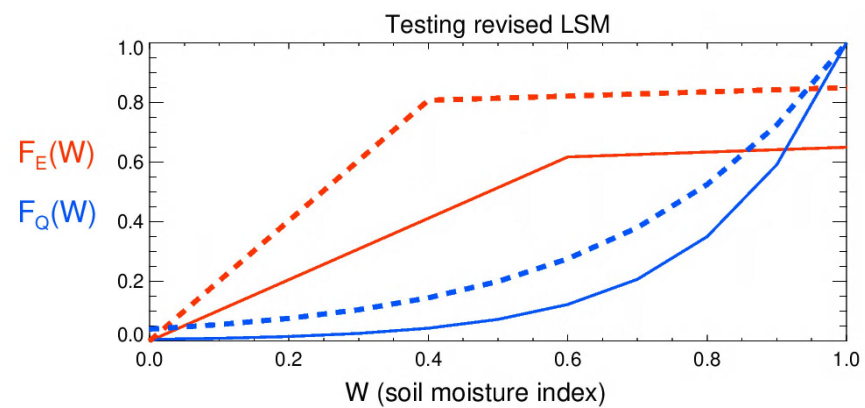
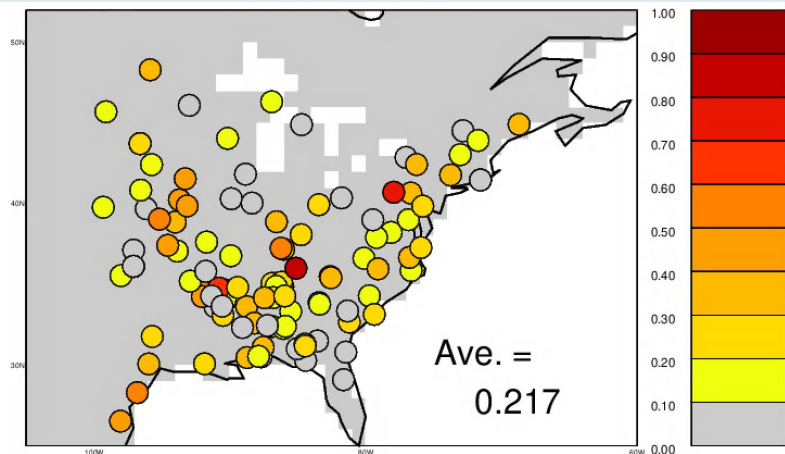
Dashed lines: inferred model curves

Solid lines: inferred Nature curves

*And now – some results from a first test, where we move the red curve a little bit in the right direction. (We're just getting started with the optimization...)*

Thanks to Yujin Zeng for initial offline testing of modification!

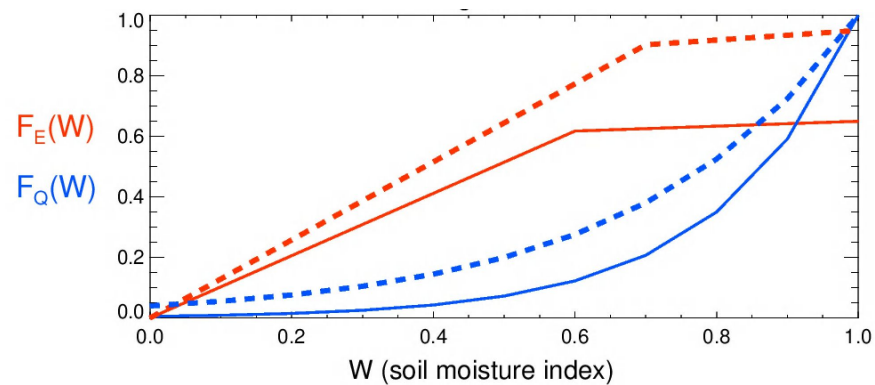
## Offline forecast skill for soil moisture ( $R^2$ )



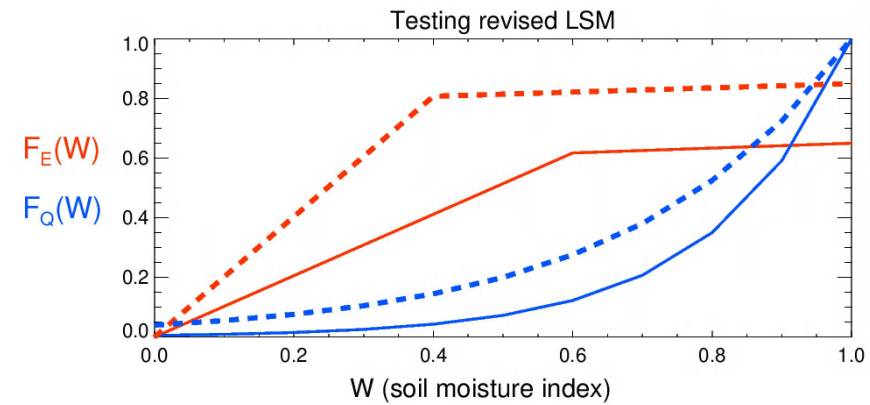
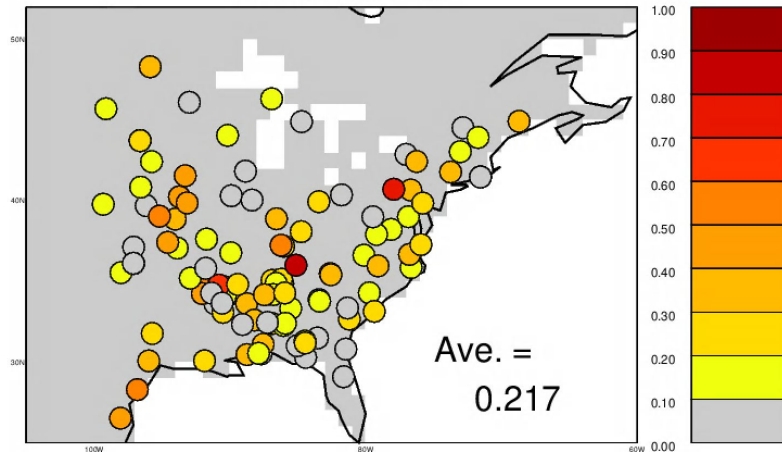
Dashed lines: inferred model curves

Solid lines: inferred Nature curves

**Modify land surface model: strengthen soil moisture stress function**



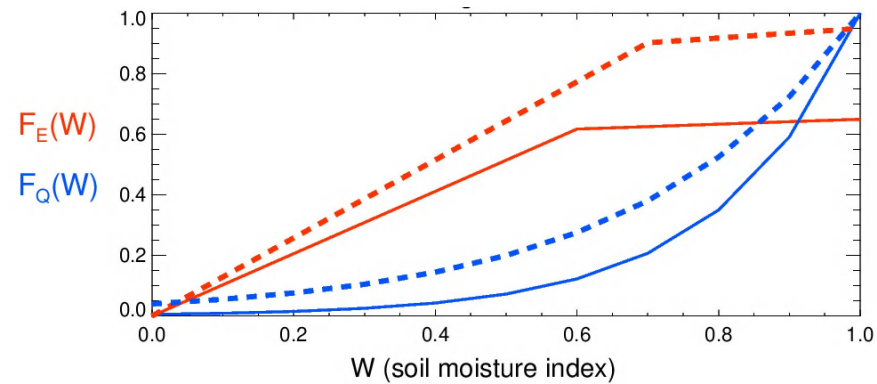
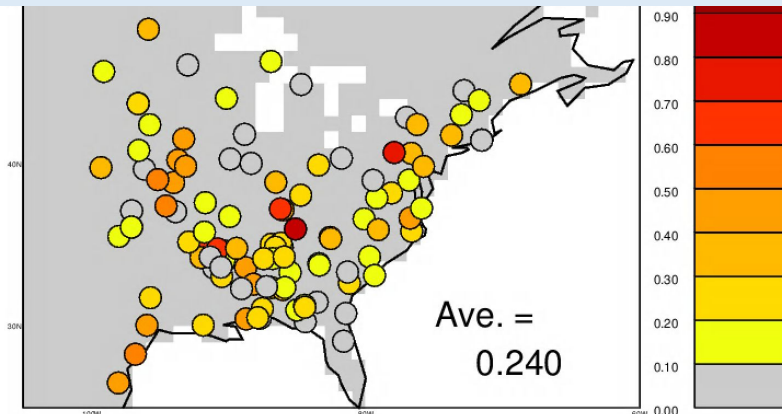
## Offline forecast skill for soil moisture ( $R^2$ )



Dashed lines: inferred model curves

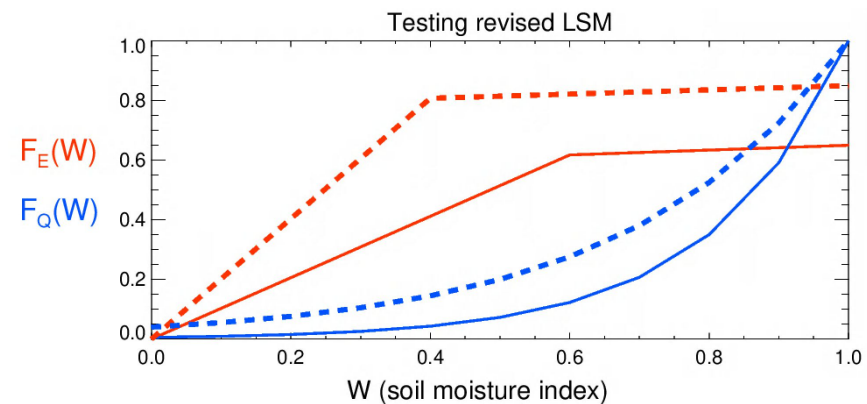
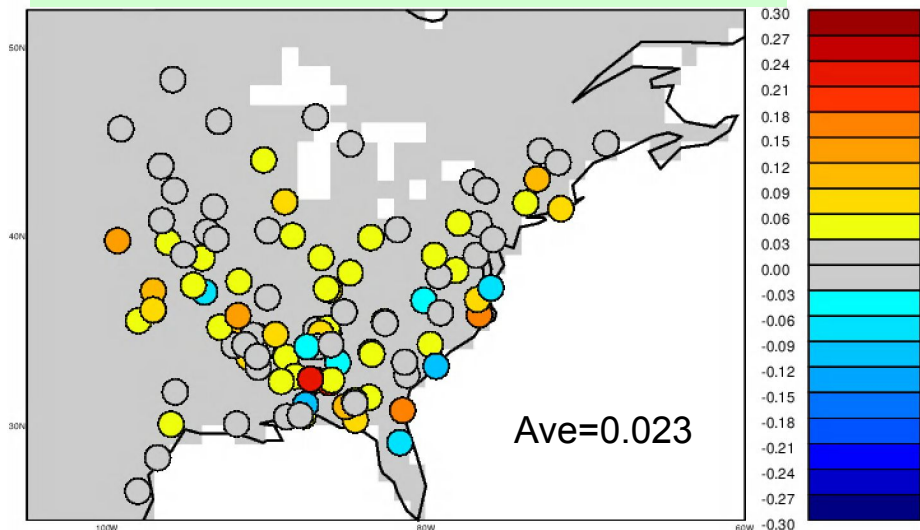
Solid lines: inferred Nature curves

## Offline forecast skill for soil moisture ( $R^2$ ); revised model



**Modify land surface model: strengthen soil moisture stress function**

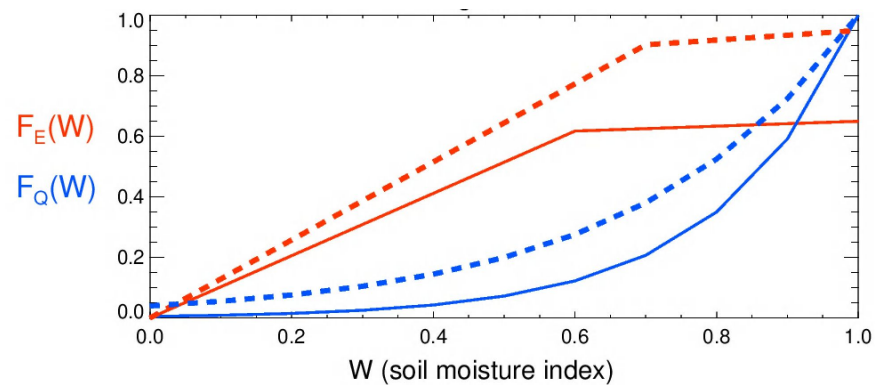
Differences: Increase in skill due to model revision



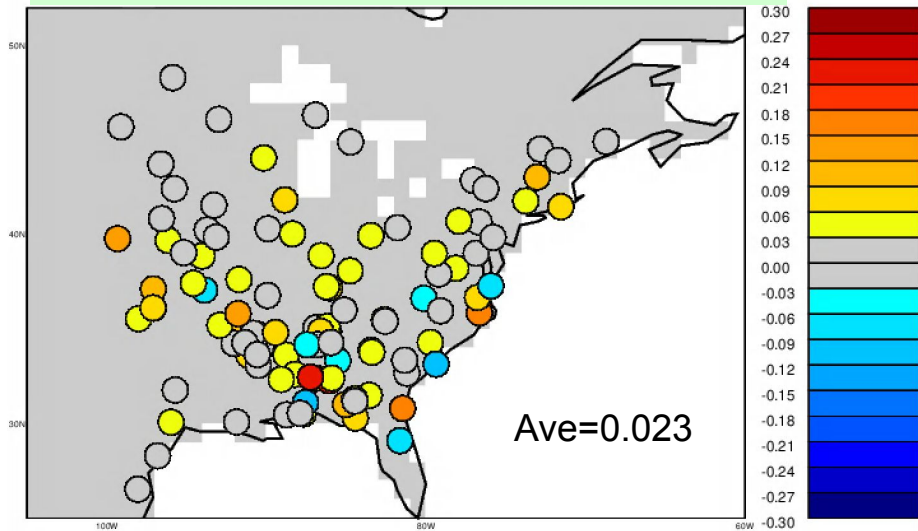
Dashed lines: inferred model curves

Solid lines: inferred Nature curves

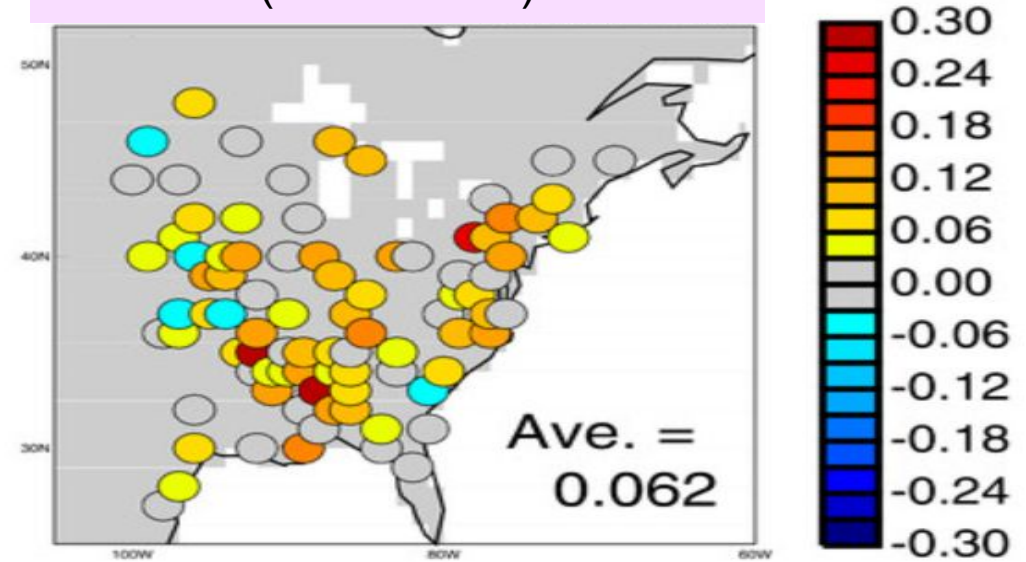
Modify land surface model: strengthen soil moisture stress function



### Differences: Increase in skill due to model revision



### Potential increases in skill, based on “bare bones” analysis (from before)



<https://doi.org/10.1175/JHM-D-22-0050.1>





This experiment also led to a much-smaller-in-magnitude *degradation* of streamflow prediction skill. Overall, there was still an improvement in forecast hydrology

Again, this was only our first test...

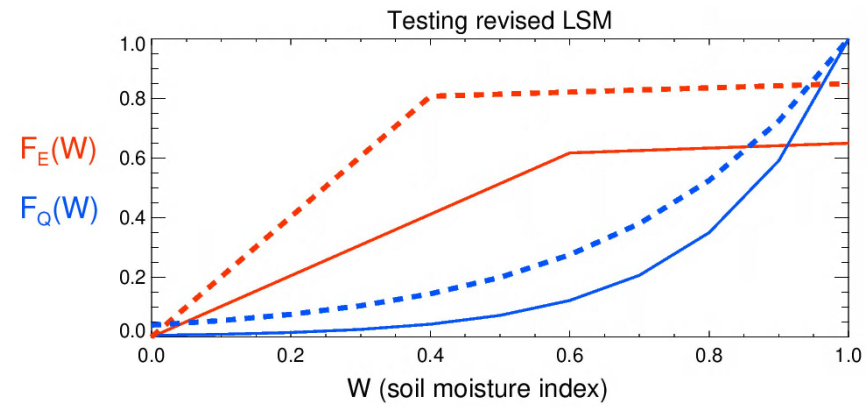
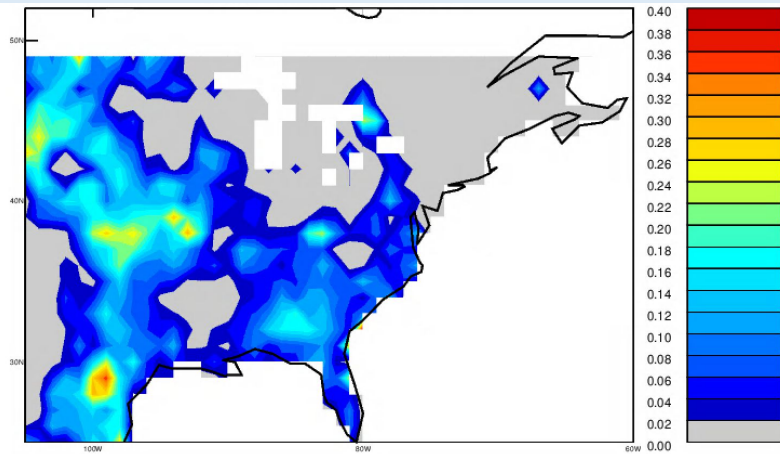


This experiment also led to a much-smaller-in-magnitude *degradation* of streamflow prediction skill. Overall, there was still an improvement in forecast hydrology

Again, this was only our first test...

Could the land model modification contribute to improved air temperature forecast skill, if it were put into the full S2S system? (i.e., allow land-atmosphere feedbacks?) We think so!

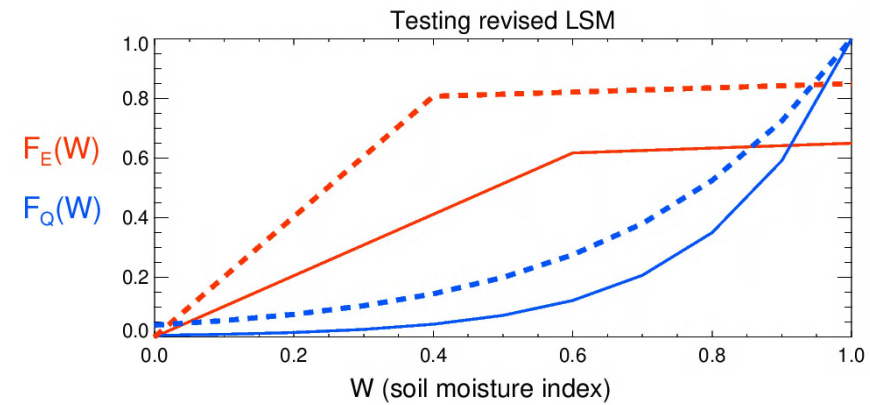
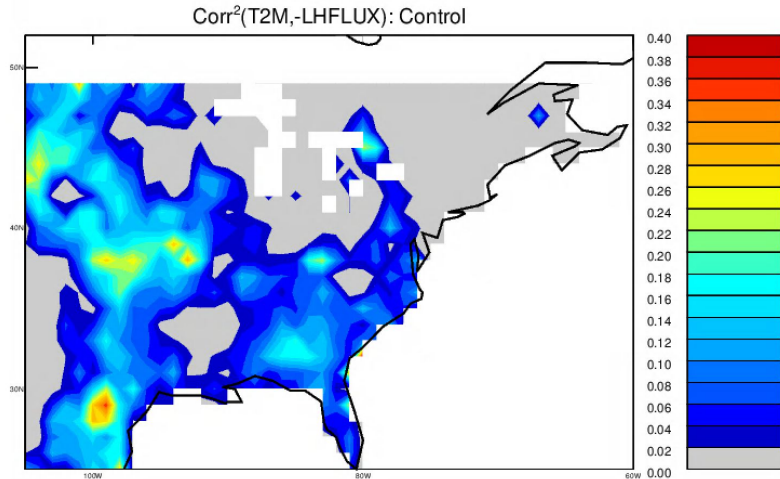
## $R^2$ between negative of forecast ET and observed day-night T2M difference



Dashed lines: inferred model curves

Solid lines: inferred Nature curves

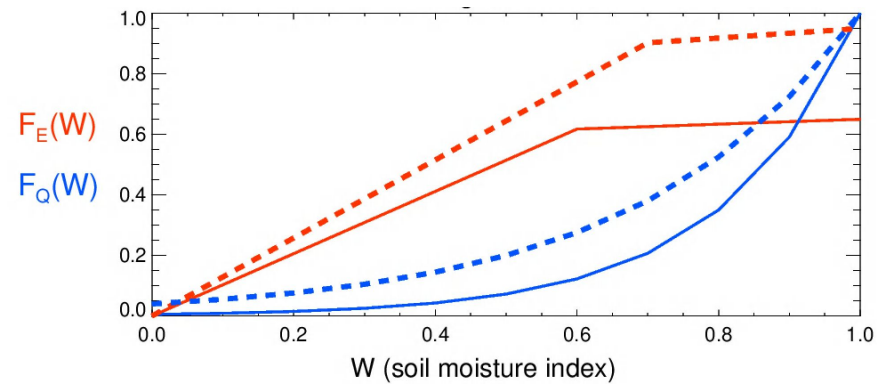
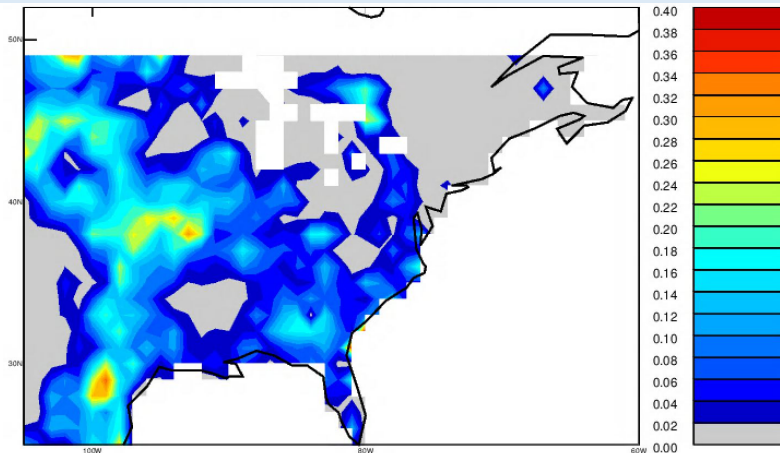
## $R^2$ between negative of forecast ET and observed day-night T2M difference



Dashed lines: inferred model curves

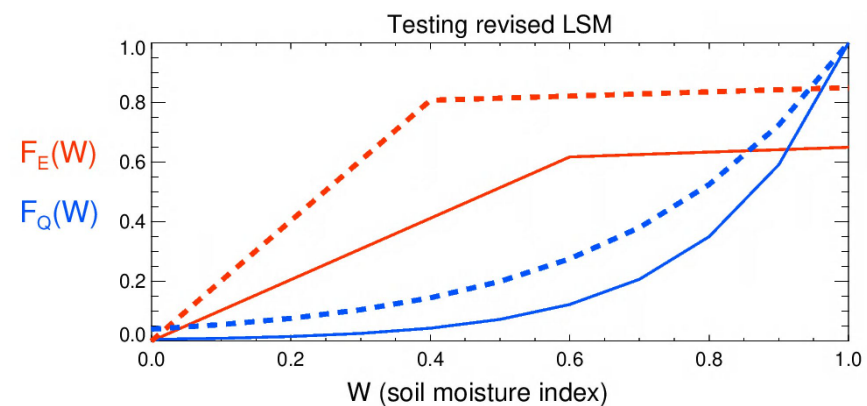
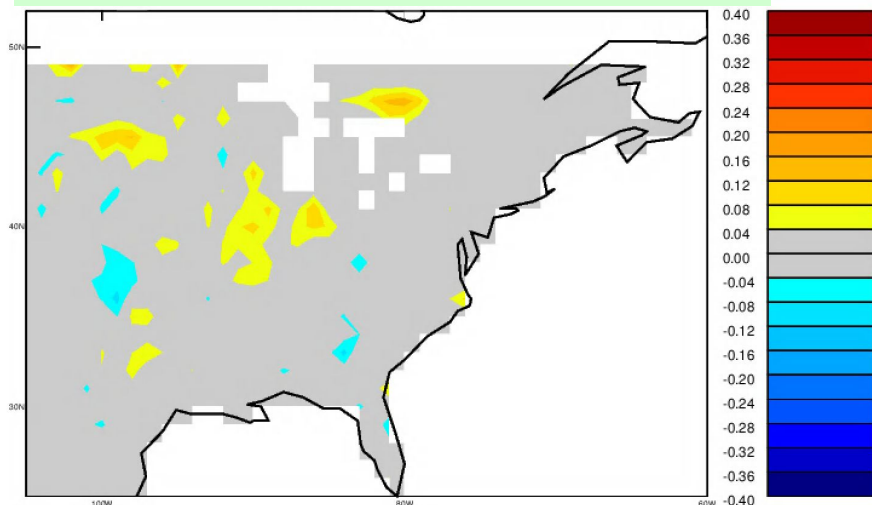
Solid lines: inferred Nature curves

## Same, but using revised land model



**Modify land surface model: strengthen soil moisture stress function**

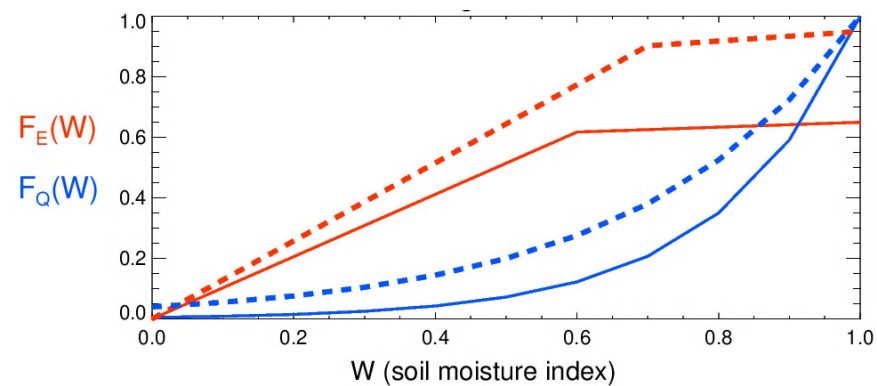
## Differences: Increase in skill due to model revision



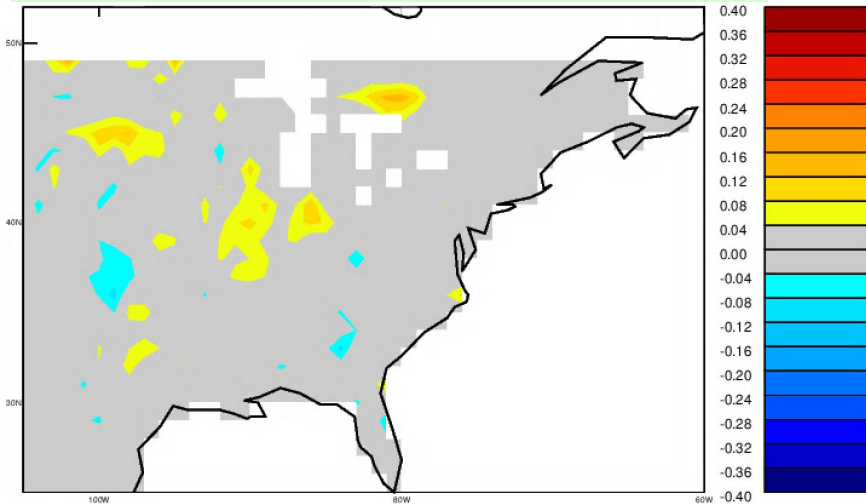
Dashed lines: inferred model curves

Solid lines: inferred Nature curves

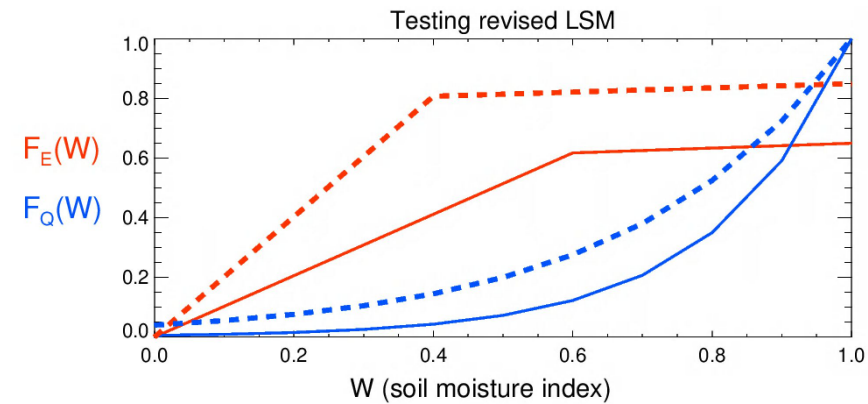
**Modify land surface model: strengthen soil moisture stress function**



## Differences: Increase in skill due to model revision



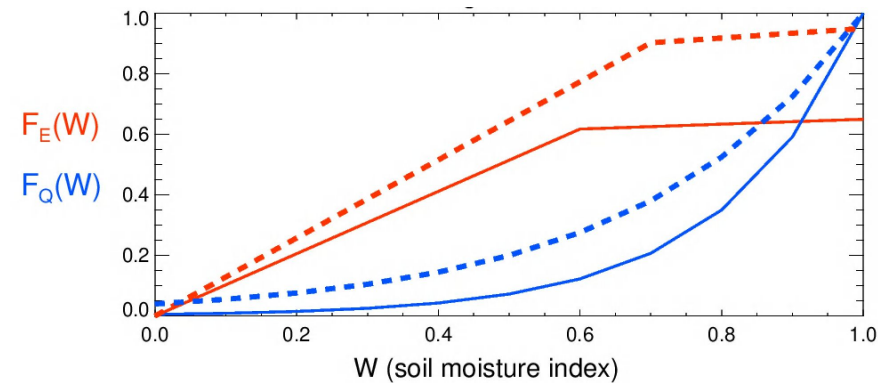
Far from conclusive – but maybe this is real! Maybe, through feedback, the land improvements would improve T2M forecasts!



Dashed lines: inferred model curves

Solid lines: inferred Nature curves

**Modify land surface model: strengthen soil moisture stress function**





## Summary

1. We performed a “bare bones” analysis with a simple water balance model to determine the ET efficiency and runoff efficiency curves that we should target for model development.
2. We have developed an offline forecast system that is driven by bias-corrected meteorological forcing from a full S2S system.
3. The offline forecast system is tractable enough for extensive hindcast experiments aimed at optimizing a land surface model for improved hydrological prediction – under the assumption that feedbacks to the atmosphere are of secondary importance (relative to land model structure) for things like soil moisture forecasts.
4. A first test of the system shows how a modification in the ET formulation does lead to expected, though small, improvements in soil moisture forecasts (anomaly  $R^2$ ) at the subseasonal lead.















## With these sets of curves in place, do a forecast analysis

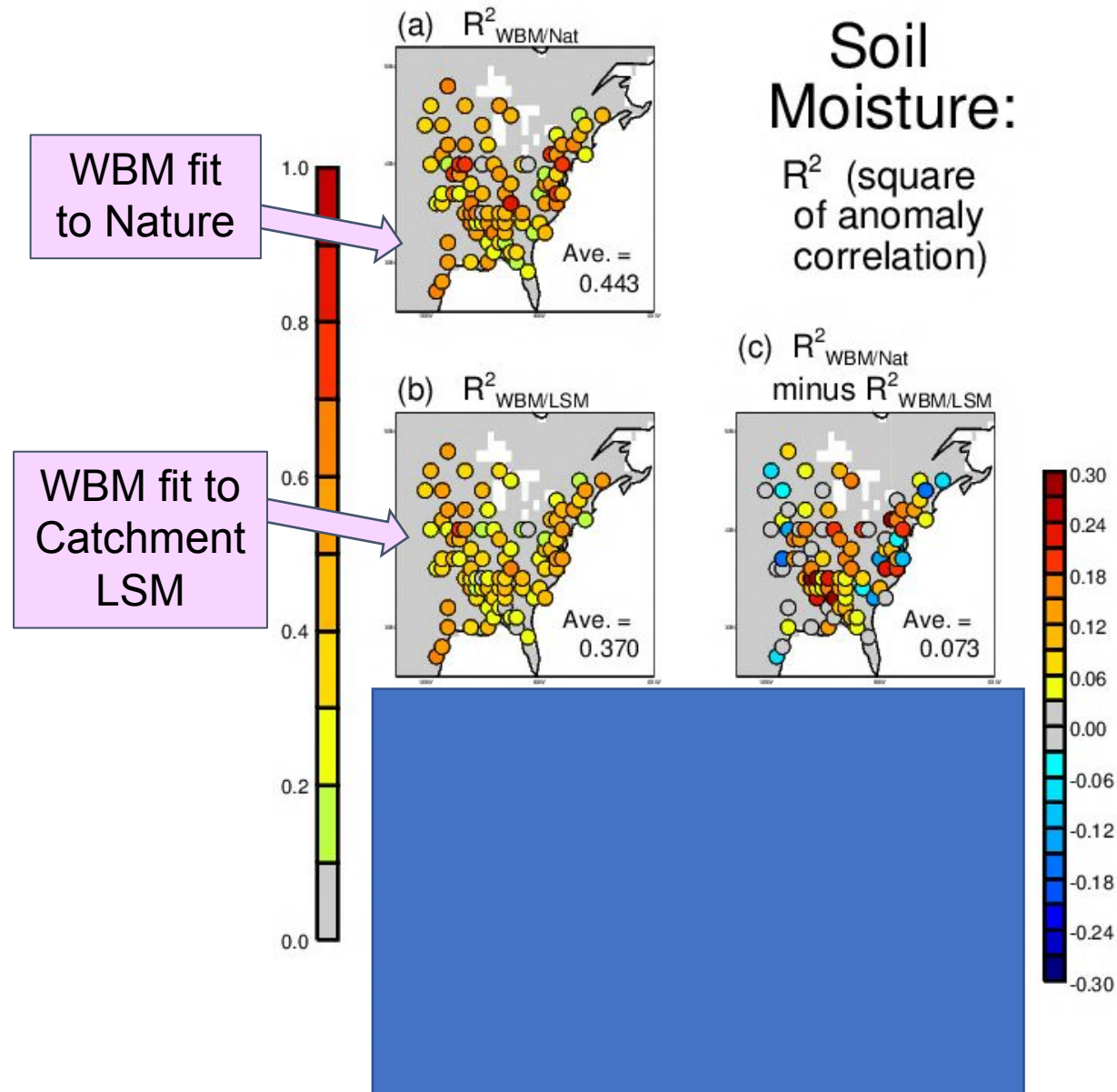
Compare warm season (May – September) offline (land-only) subseasonal forecasts of streamflow and soil moisture (at 11-20 day lead) to independent in-situ observations at a collection of measurement sites across the eastern continental US:

Two forecast experiments:

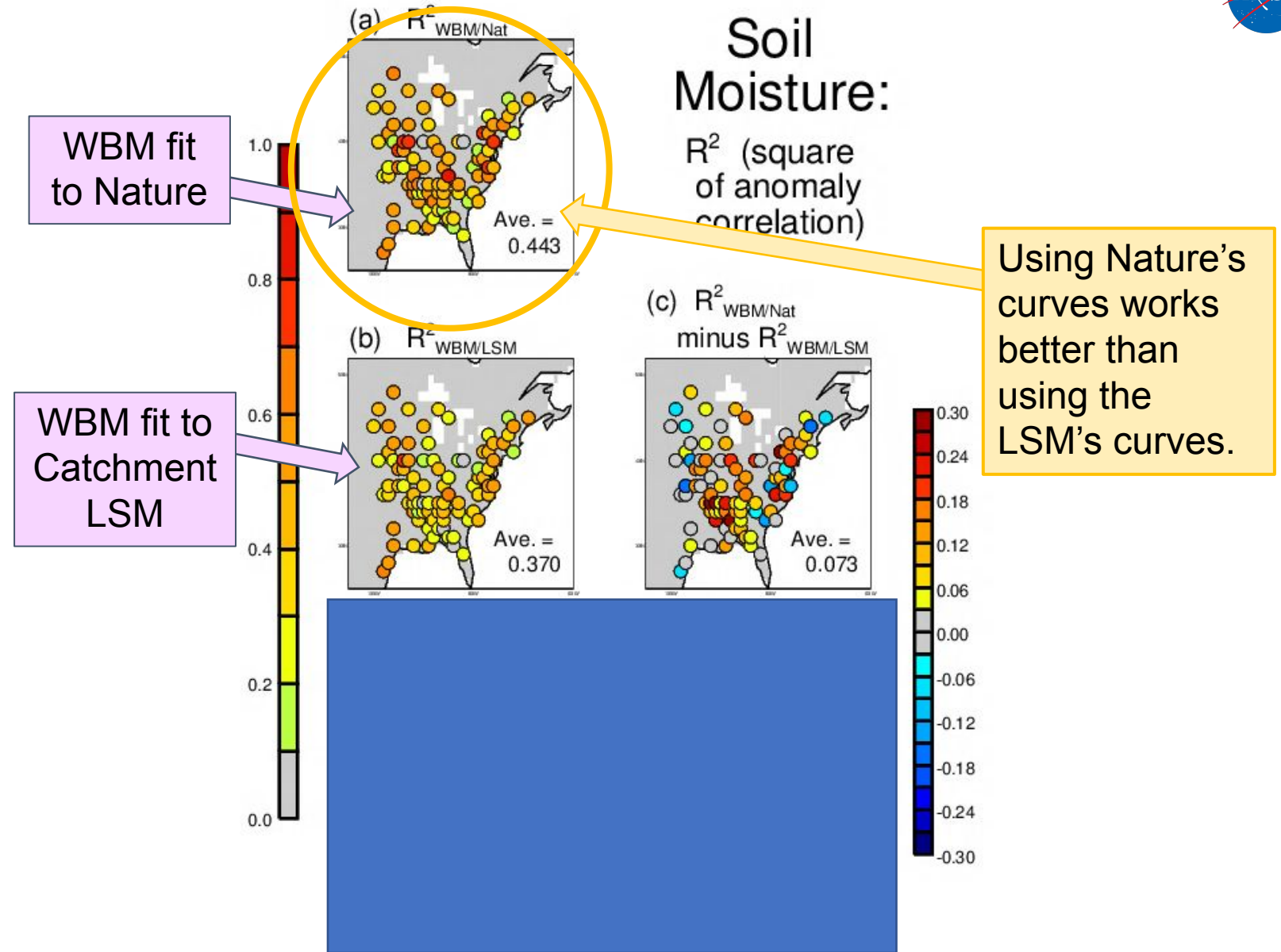
- 1) “Perfect” meteorological forcing (use observed  $P$ ,  $R_{net}$ )
- 2) “Zero-skill” meteorological forcing (use climatological  $P$ ,  $R_{net}$ )

*For full details on experimental design and more results, see:*  
[doi:10.1175/JHM-D-22-0050.1](https://doi.org/10.1175/JHM-D-22-0050.1)

*Skill ( $R^2$  vs obs.)  
assuming “perfect”  
meteorological  
forecasts – basically,  
the skill of a  
hydrological simulation  
with observed forcing.*



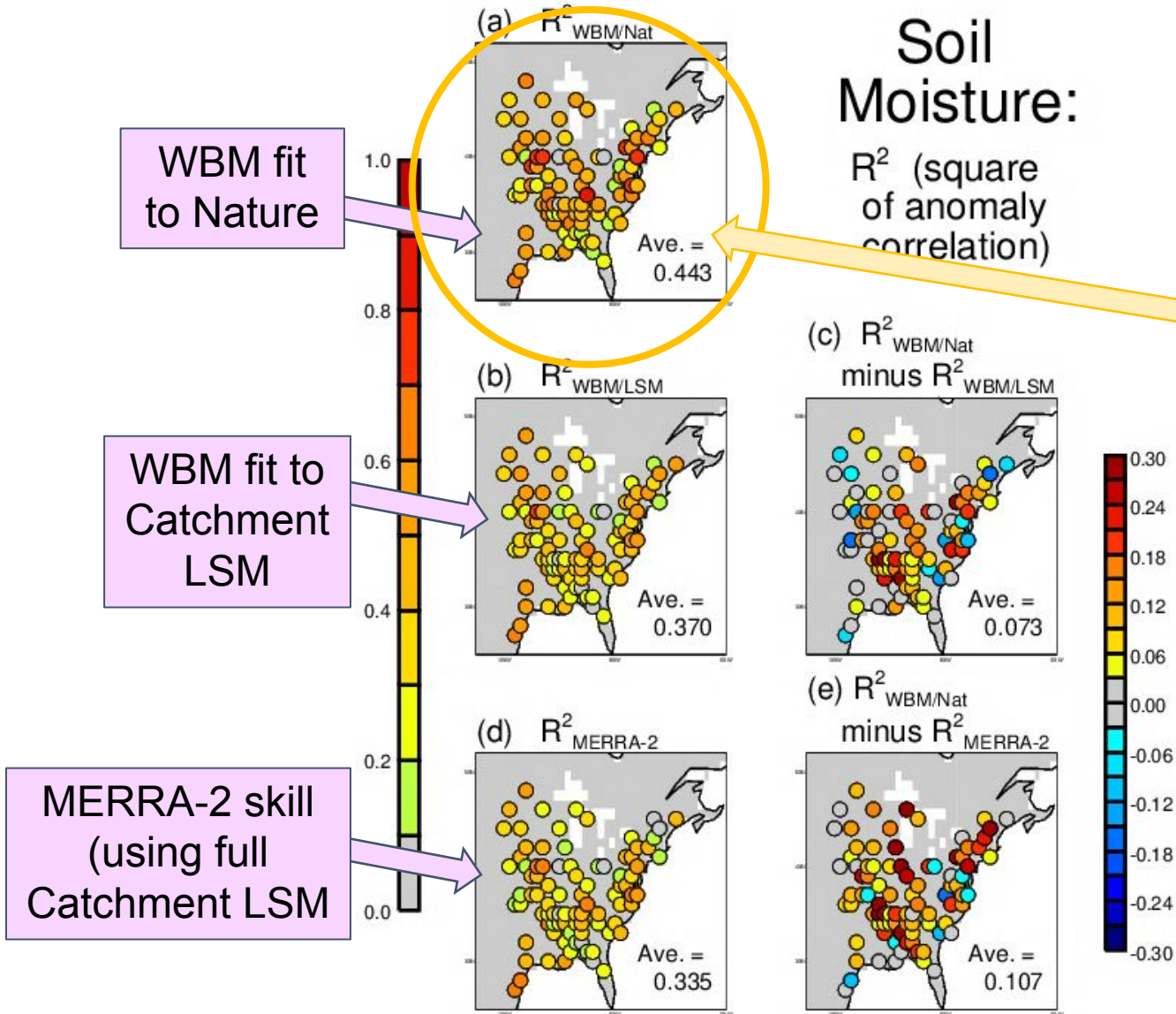
*Skill ( $R^2$  vs obs.)  
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with observed forcing.*



*Skill ( $R^2$  vs obs.) assuming “perfect” meteorological forecasts – basically, the skill of a hydrological simulation with observed forcing*

## Soil Moisture:

$R^2$  (square of anomaly correlation)





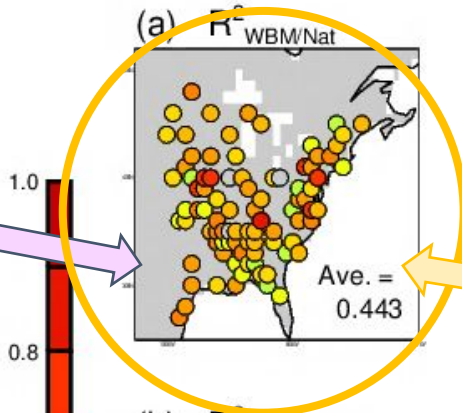
*Skill ( $R^2$  vs obs.) assuming “perfect” meteorological forecasts – basically, the skill of a hydrological simulation with observed forcing*

**Results for streamflow are similar!**

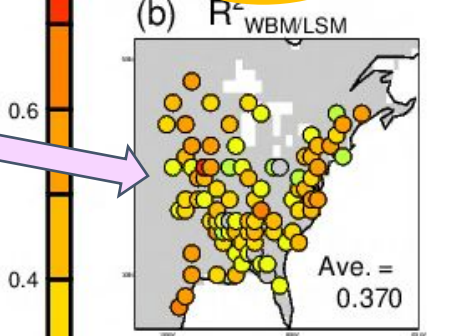
# Soil Moisture:

$R^2$  (square of anomaly correlation)

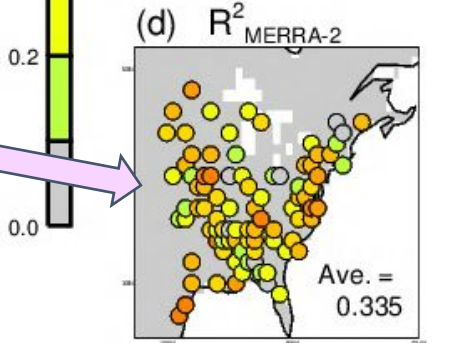
WBM fit to Nature



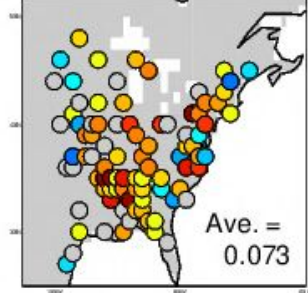
WBM fit to Catchment LSM



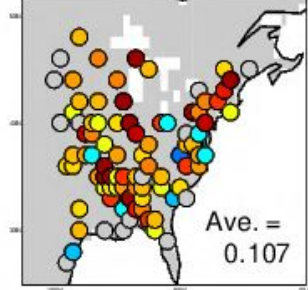
MERRA-2 skill (using full Catchment LSM)



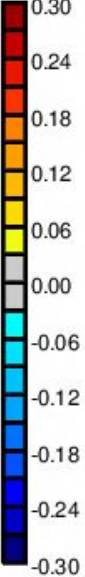
(c)  $R^2_{WBM/Nat}$  minus  $R^2_{WBM/LSM}$



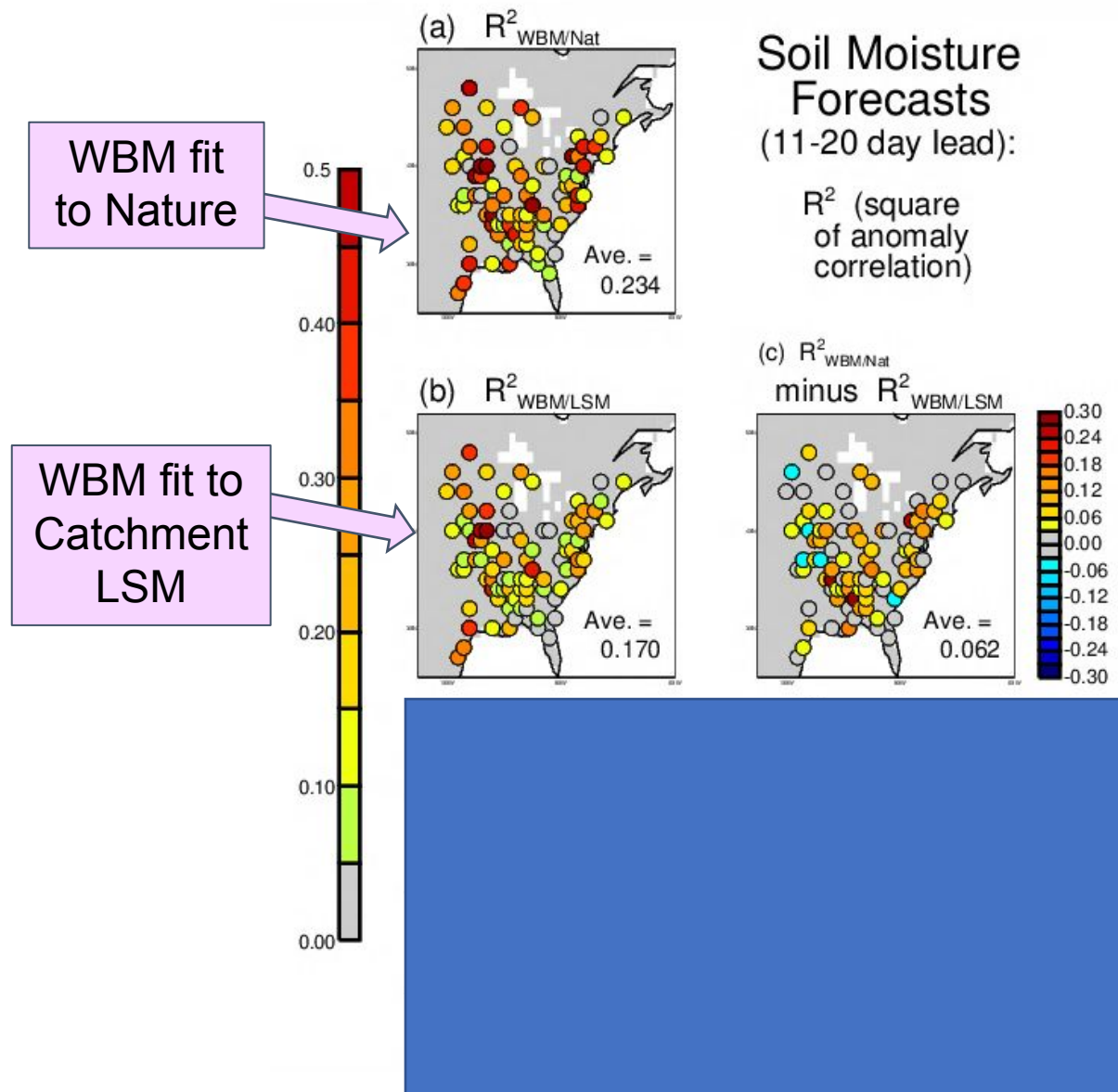
(e)  $R^2_{WBM/Nat}$  minus  $R^2_{MERRA-2}$



Using Nature’s curves works better than using the LSM’s curves.



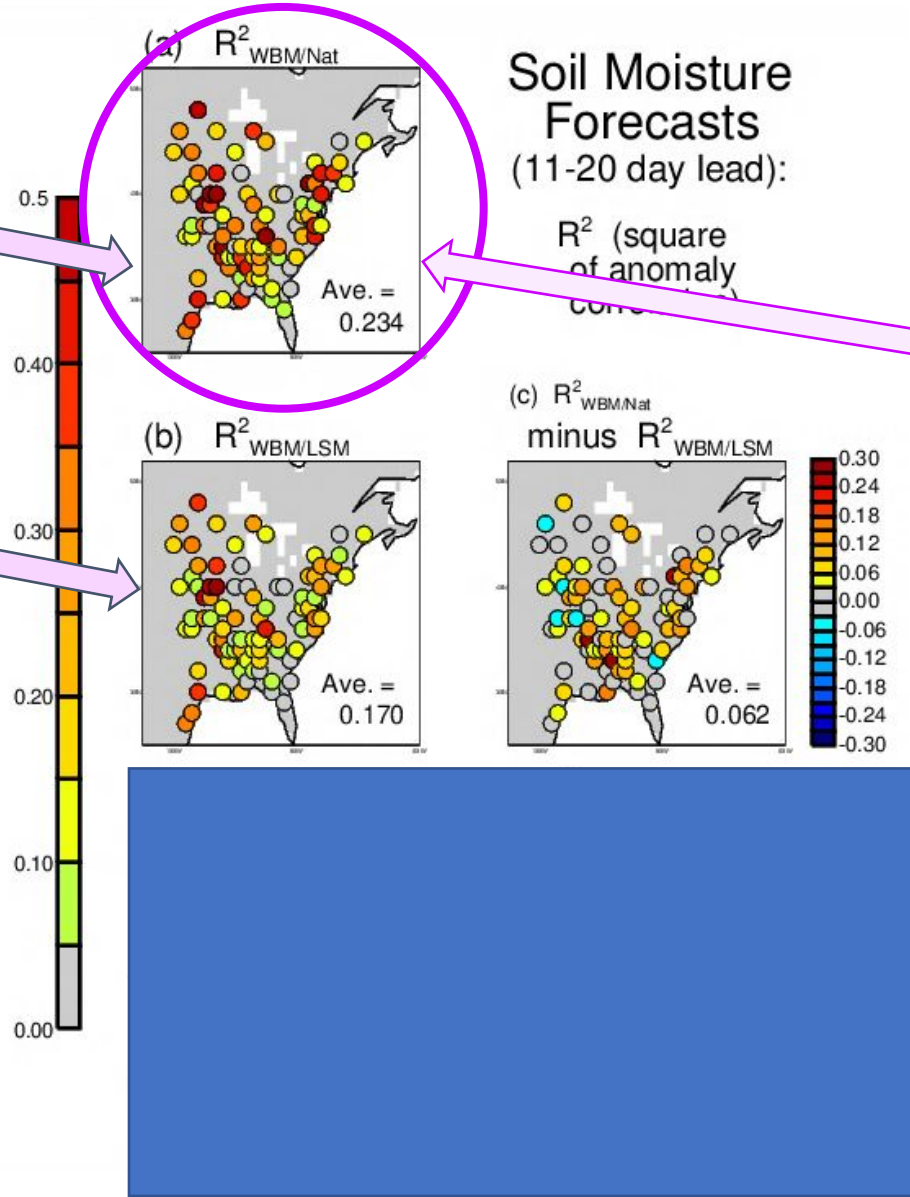
*Skill ( $R^2$  vs obs.)  
assuming zero-skill  
meteorological  
forecasts  
(climatological  $P$ ,  $R_{net}$   
during the forecast  
period)*



*Skill ( $R^2$  vs obs.)  
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 (climatological  $P$ ,  $R_{net}$   
 during the forecast  
 period)*

WBM fit  
 to Nature

WBM fit to  
 Catchment  
 LSM

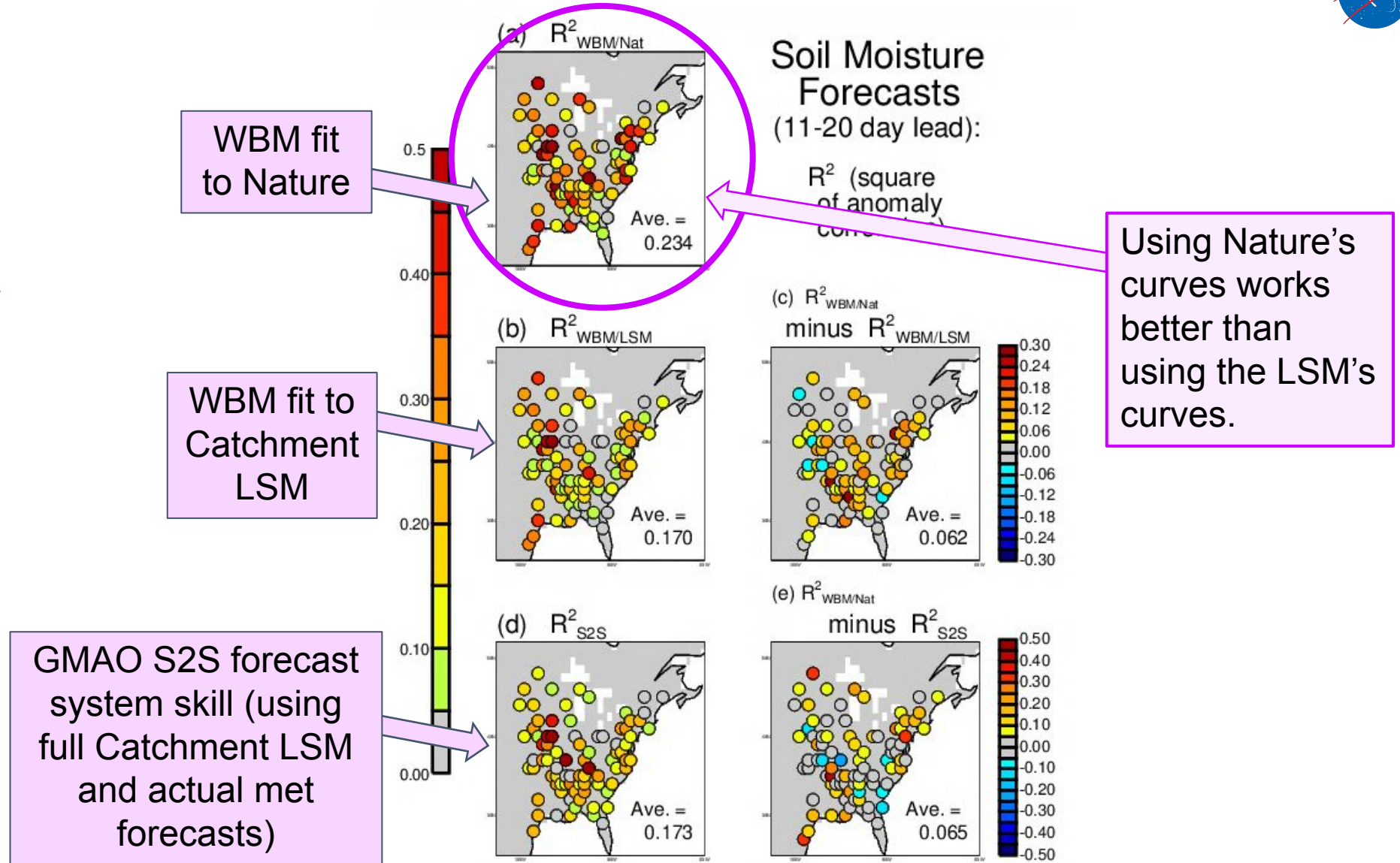


Soil Moisture  
 Forecasts  
 (11-20 day lead):

$R^2$  (square  
 of anomaly  
 correlation)

Using Nature's  
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*Skill ( $R^2$  vs obs.)  
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forecasts  
(climatological  $P$ ,  $R_{net}$   
during the forecast  
period)*



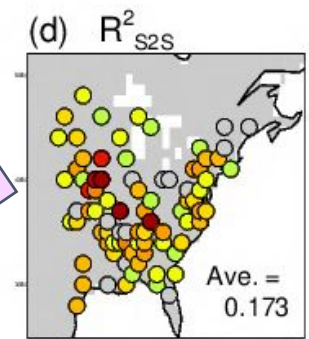
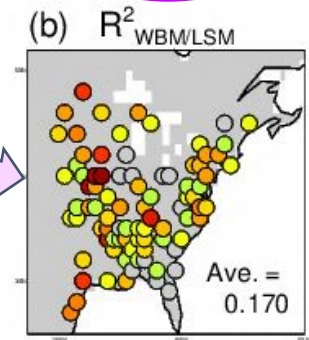
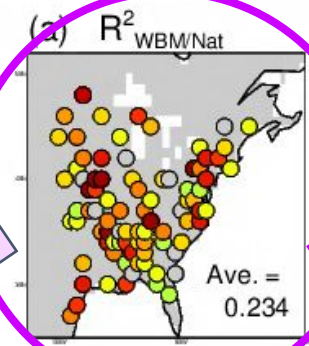
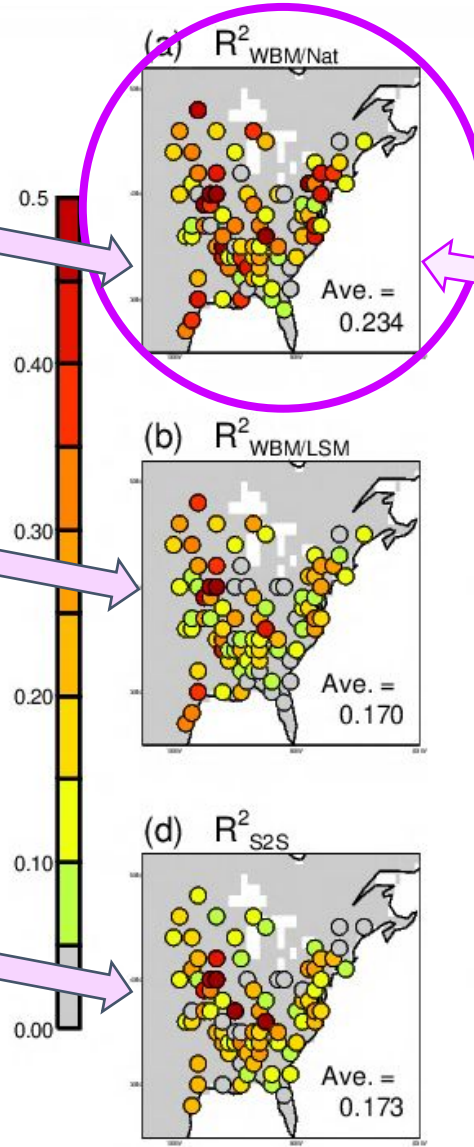
*Skill ( $R^2$  vs obs.)  
assuming zero-skill  
meteorological  
forecasts  
(climatological  $P$ ,  $R_{net}$   
during the forecast  
period)*

**Results for  
streamflow  
are similar!**

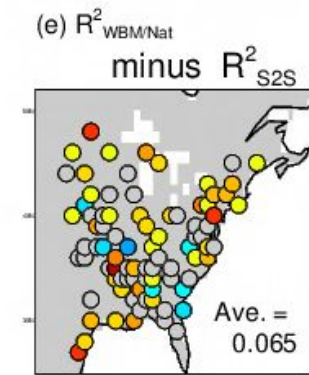
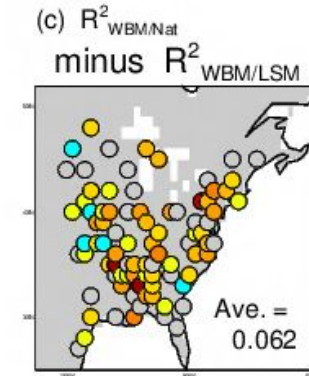
GMAO S2S forecast  
system skill (using  
full Catchment LSM  
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forecasts)

WBM fit  
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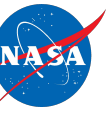
WBM fit to  
Catchment  
LSM



Soil Moisture  
Forecasts  
(11-20 day lead):  
 $R^2$  (square  
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coeff.)



Using Nature's  
curves works  
better than  
using the LSM's  
curves.



Approach: Examine problem with a “bare bones” representation of a land surface model.

# Bare-bones representation: the “WBM”, based on water balance equation

Soil profile water  
holding capacity

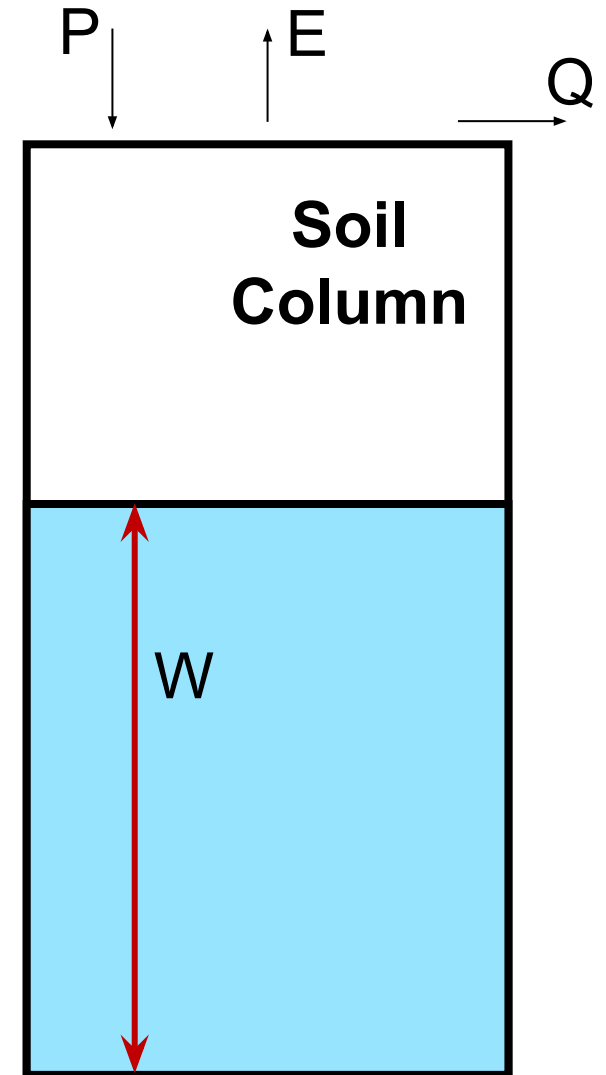
Precipitation

Evapotranspiration

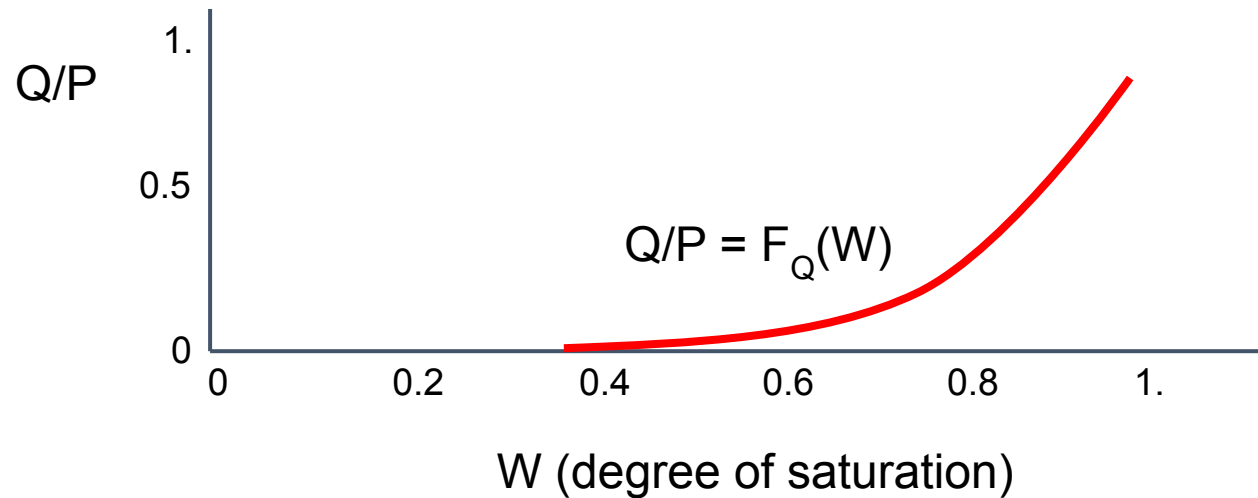
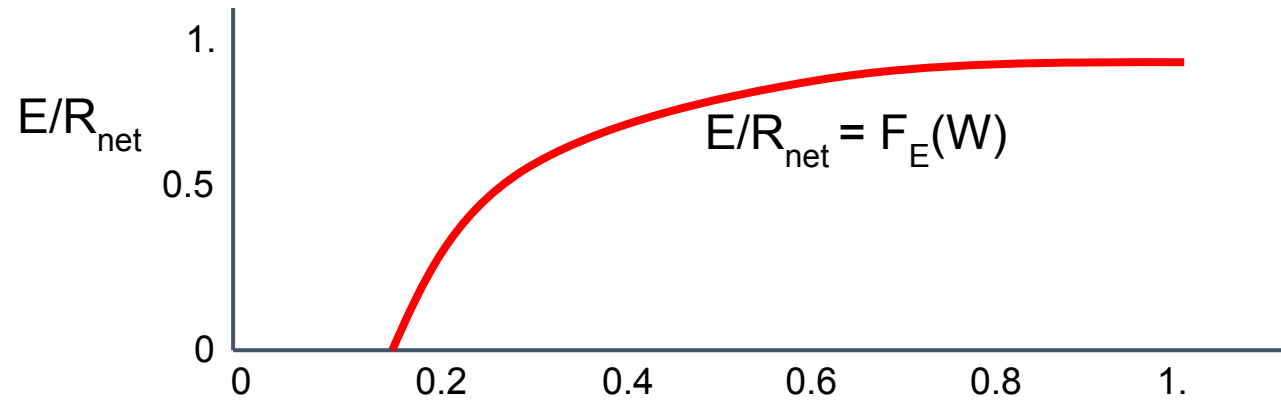
$$C W_{n+1} = C W_n + P_n - E_n - Q_n,$$

Total runoff

Soil moisture at start of day n (degree of saturation)



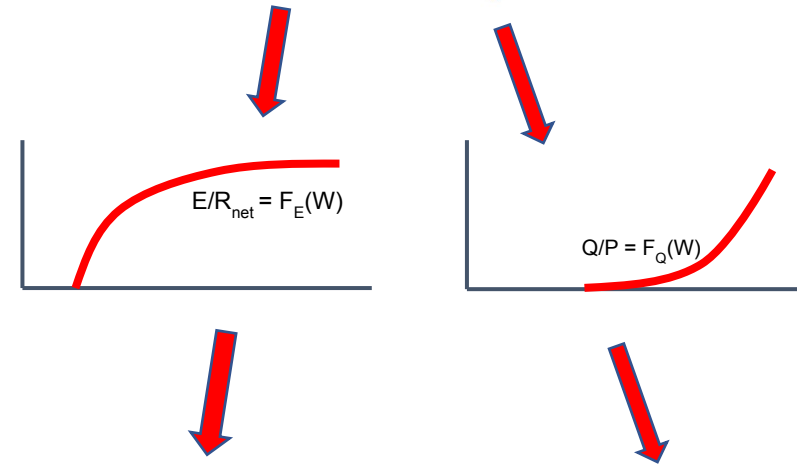
We can impose simple relationships between  $W$  and both  $E$  and  $Q$ :





□ Replace

$$C W_{n+1} = C W_n + P_n - E_n - Q_n$$

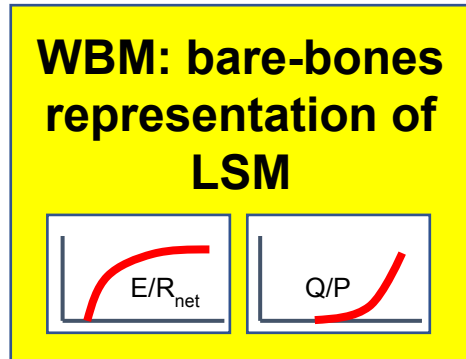
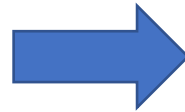


with

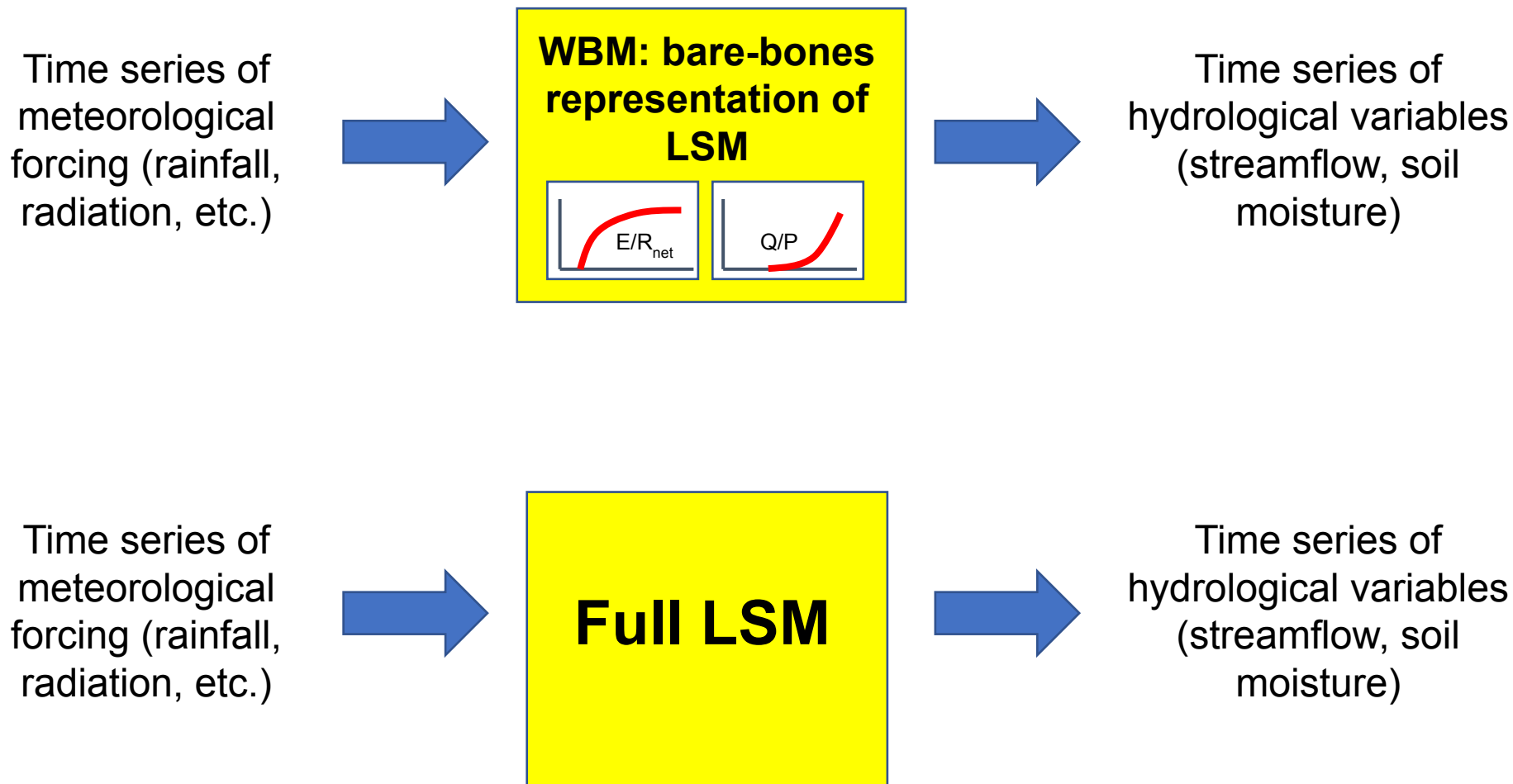
$$C W_{n+1} = C W_n + P_n - F_E(W_n) R_{\text{net-n}} - F_Q(W_n) P_n$$

This, in a nutshell, is the bare-bones representation.

Time series of meteorological forcing (rainfall, radiation, etc.)

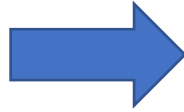


Time series of hydrological variables (streamflow, soil moisture)



*Can we calibrate the WBM curves so that this...*

Time series of meteorological forcing (rainfall, radiation, etc.)



**WBM: bare-bones representation of LSM**

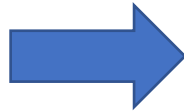


Time series of hydrological variables (streamflow, soil moisture)



*...looks like this?*

Time series of meteorological forcing (rainfall, radiation, etc.)



**Full LSM**



Time series of hydrological variables (streamflow, soil moisture)



## With these sets of curves in place, do a forecast analysis

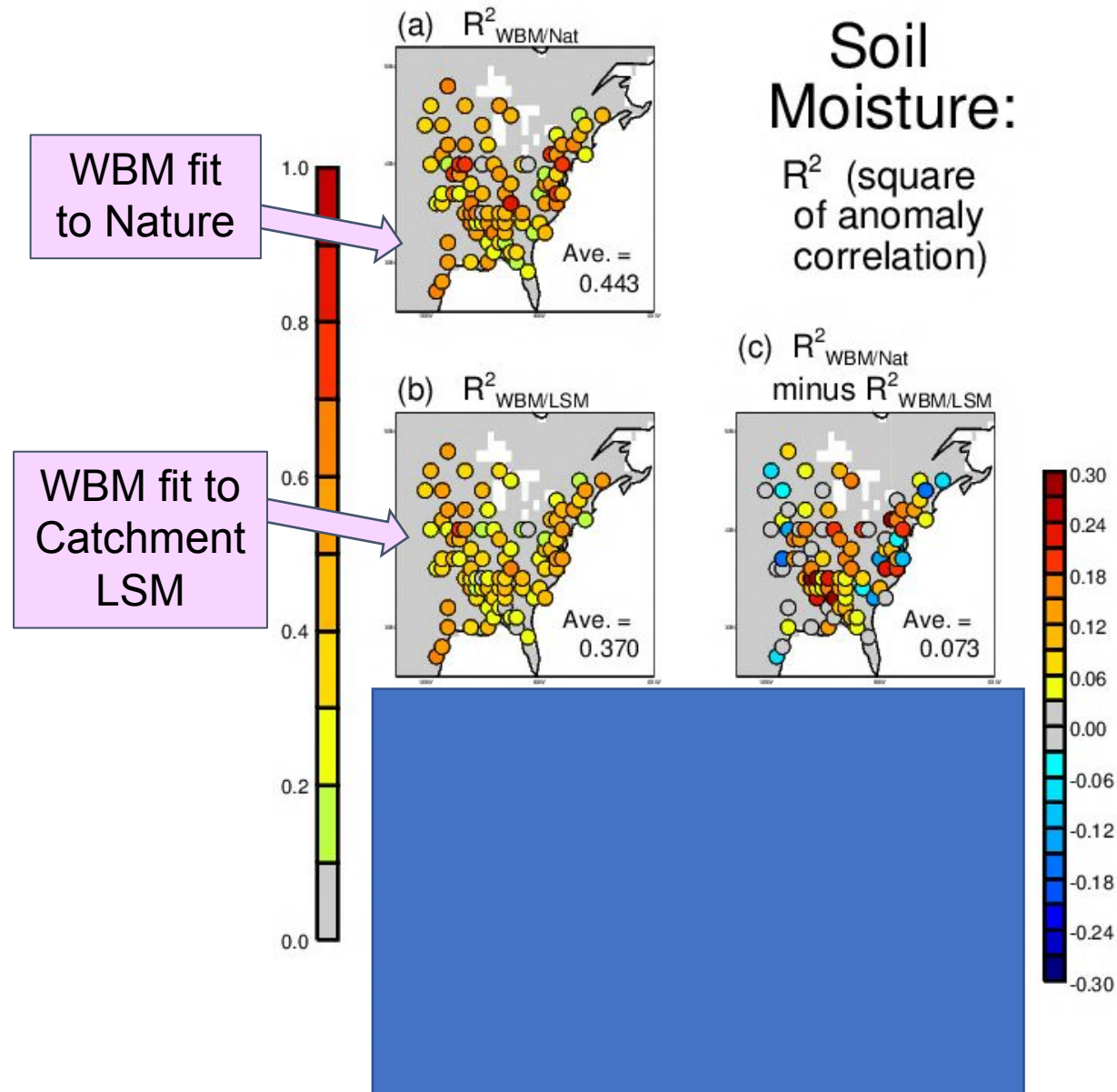
Compare warm season (May – September) offline (land-only) subseasonal forecasts of streamflow and soil moisture (at 11-20 day lead) to independent in-situ observations at a collection of measurement sites across the eastern continental US:

Two forecast experiments:

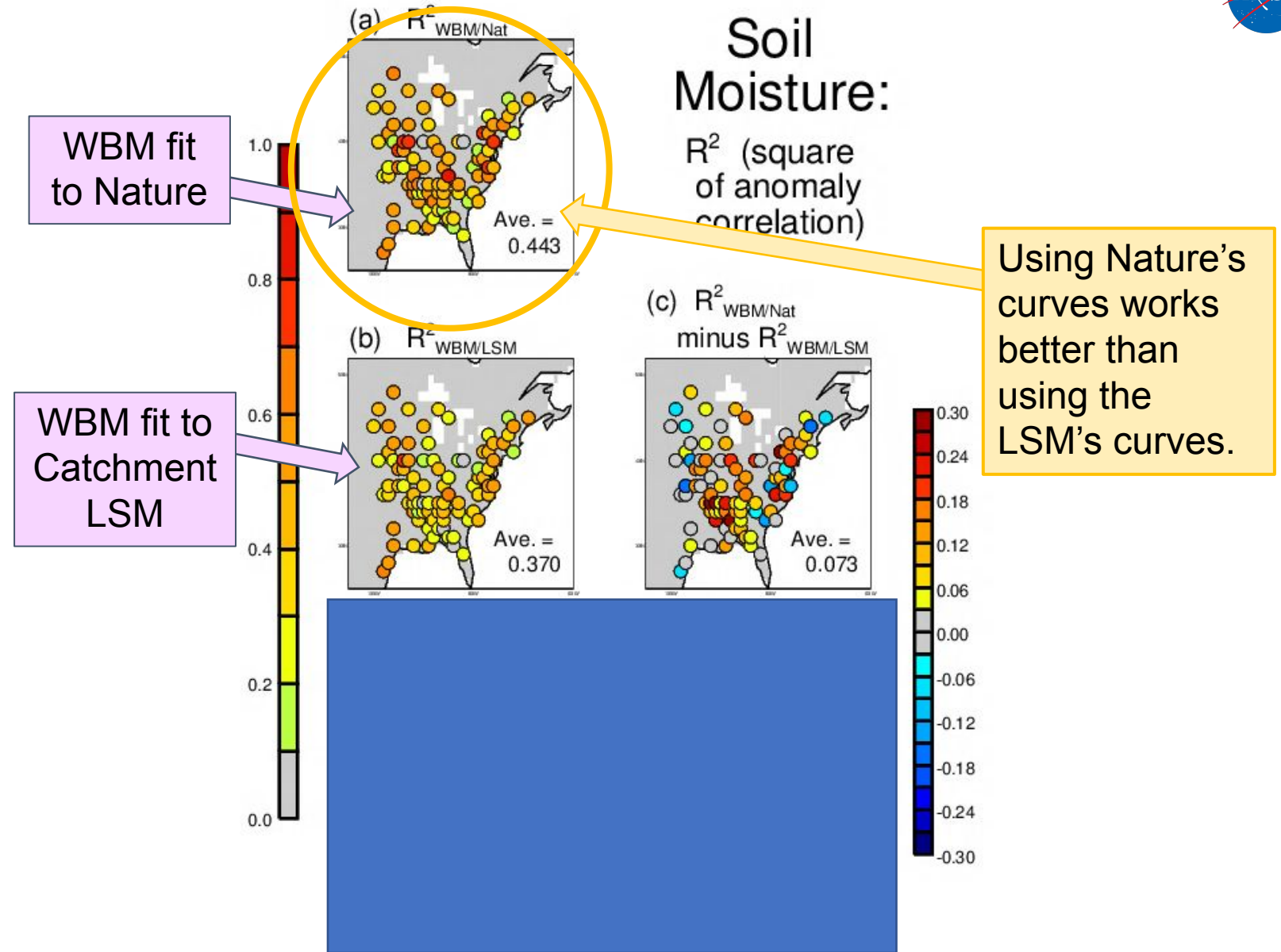
- 1) “Perfect” meteorological forcing (use observed  $P$ ,  $R_{net}$ )
- 2) “Zero-skill” meteorological forcing (use climatological  $P$ ,  $R_{net}$ )

*For full details on experimental design and more results, see:*  
[doi:10.1175/JHM-D-22-0050.1](https://doi.org/10.1175/JHM-D-22-0050.1)

*Skill ( $R^2$  vs obs.)  
assuming “perfect”  
meteorological  
forecasts – basically,  
the skill of a  
hydrological simulation  
with observed forcing.*



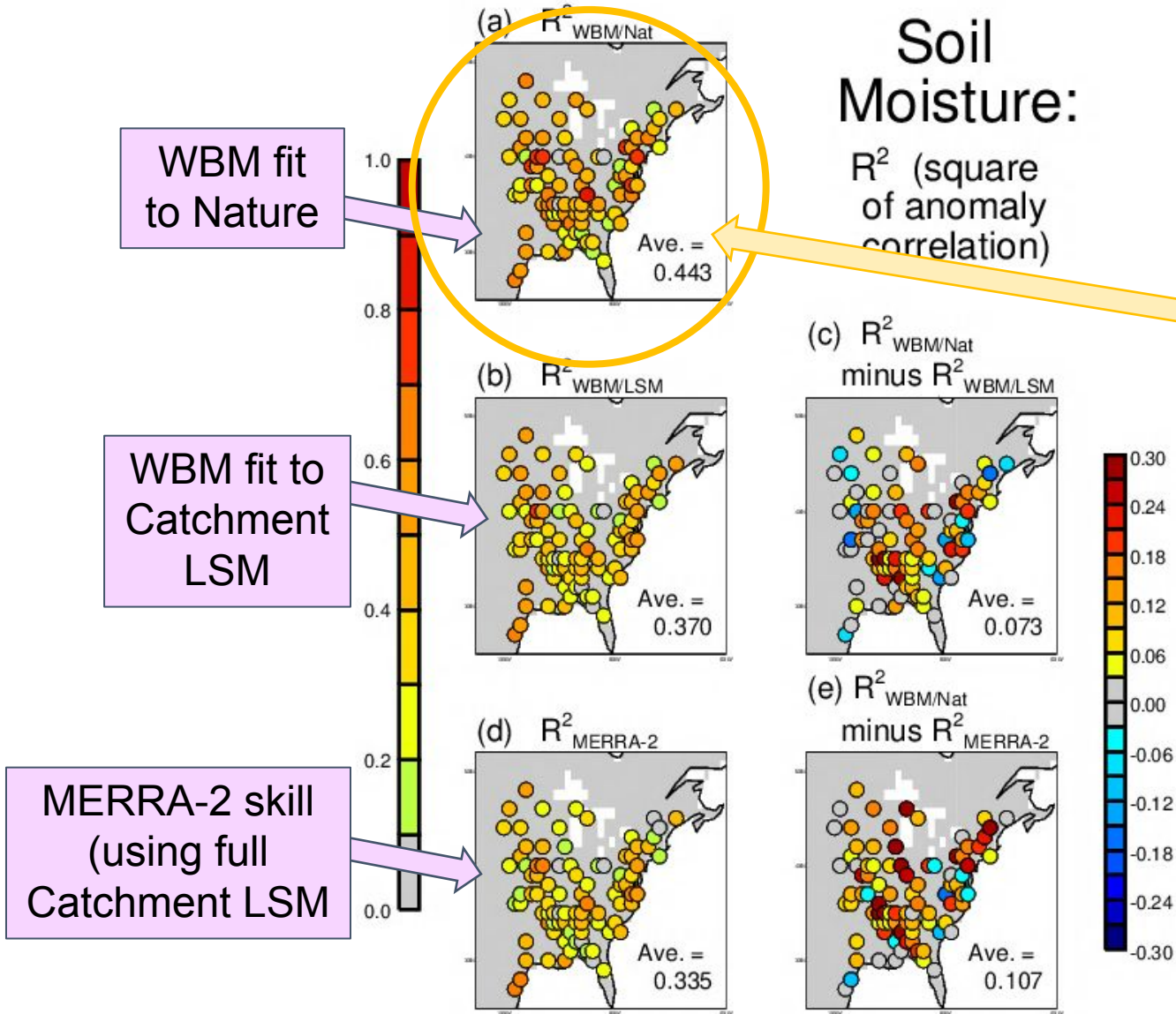
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## Soil Moisture:

$R^2$  (square of anomaly correlation)



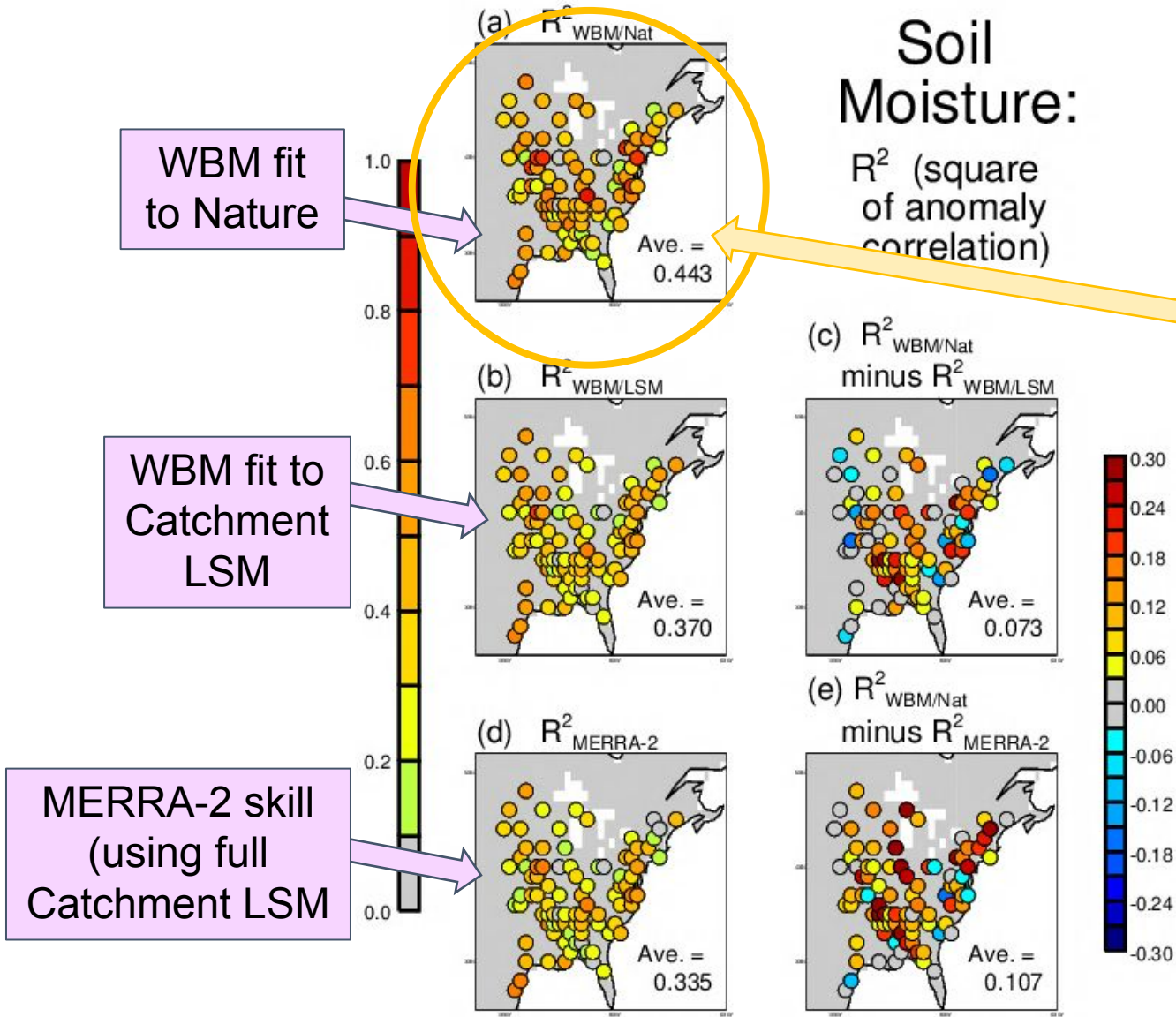


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**Results for streamflow are similar!**

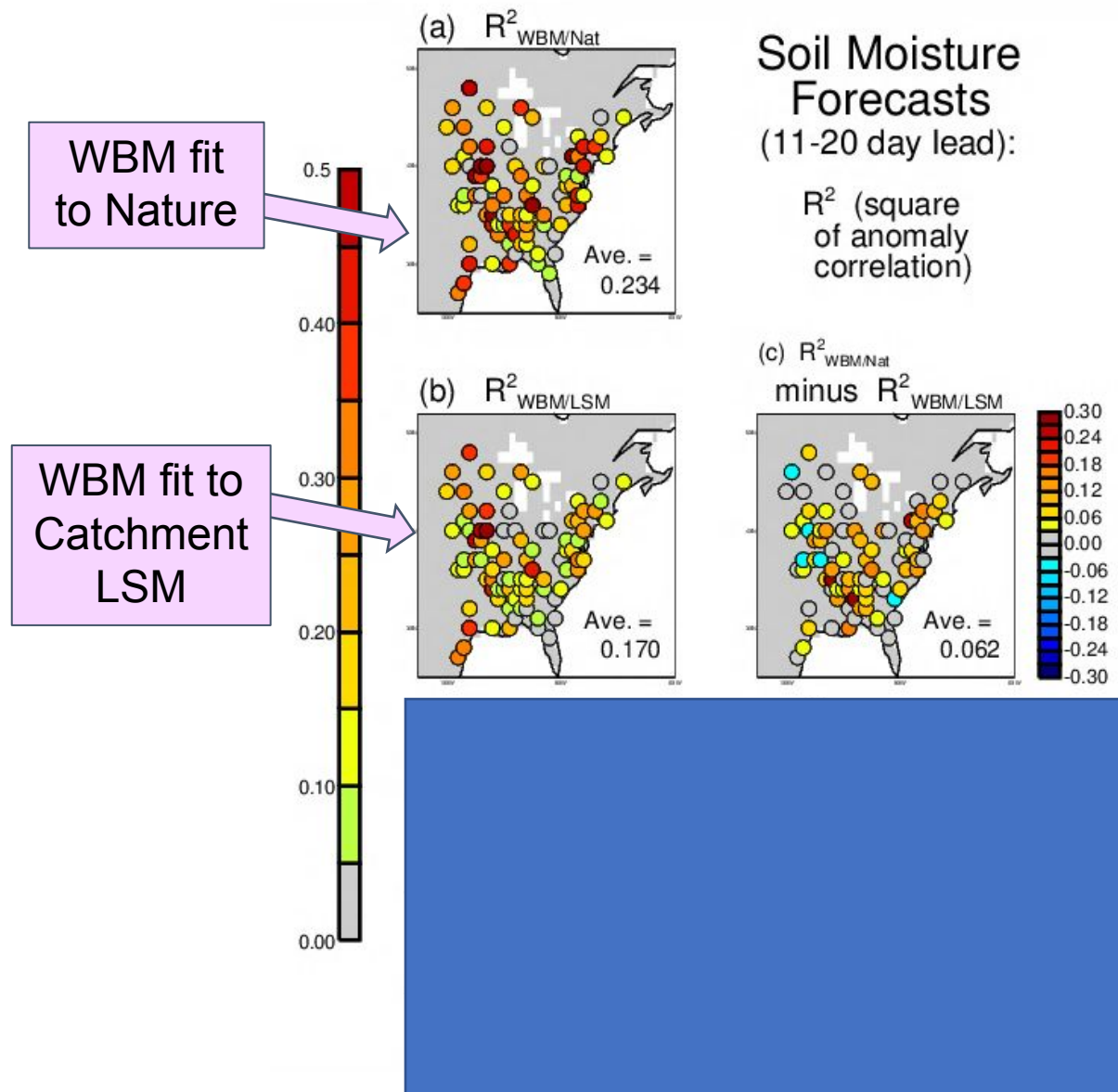
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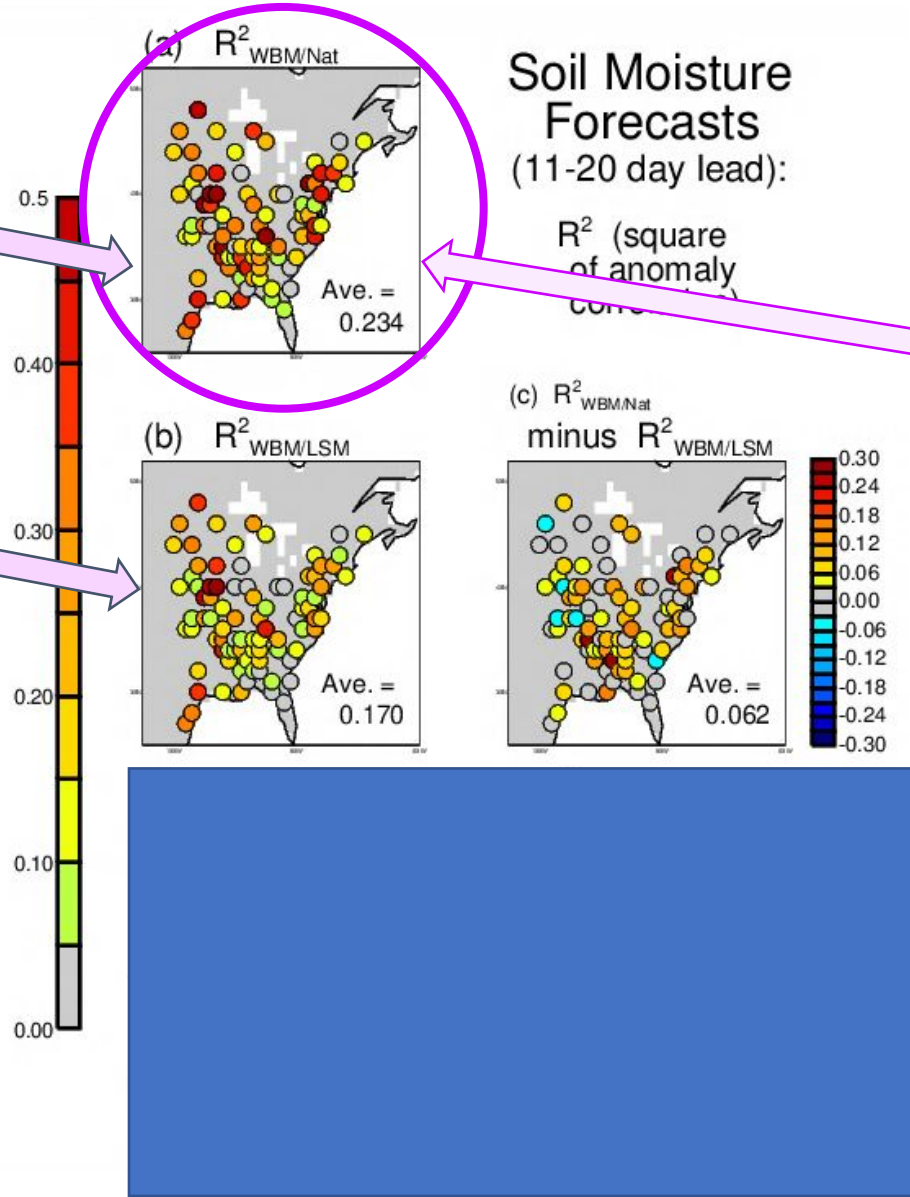
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period)*



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WBM fit  
 to Nature

WBM fit to  
 Catchment  
 LSM

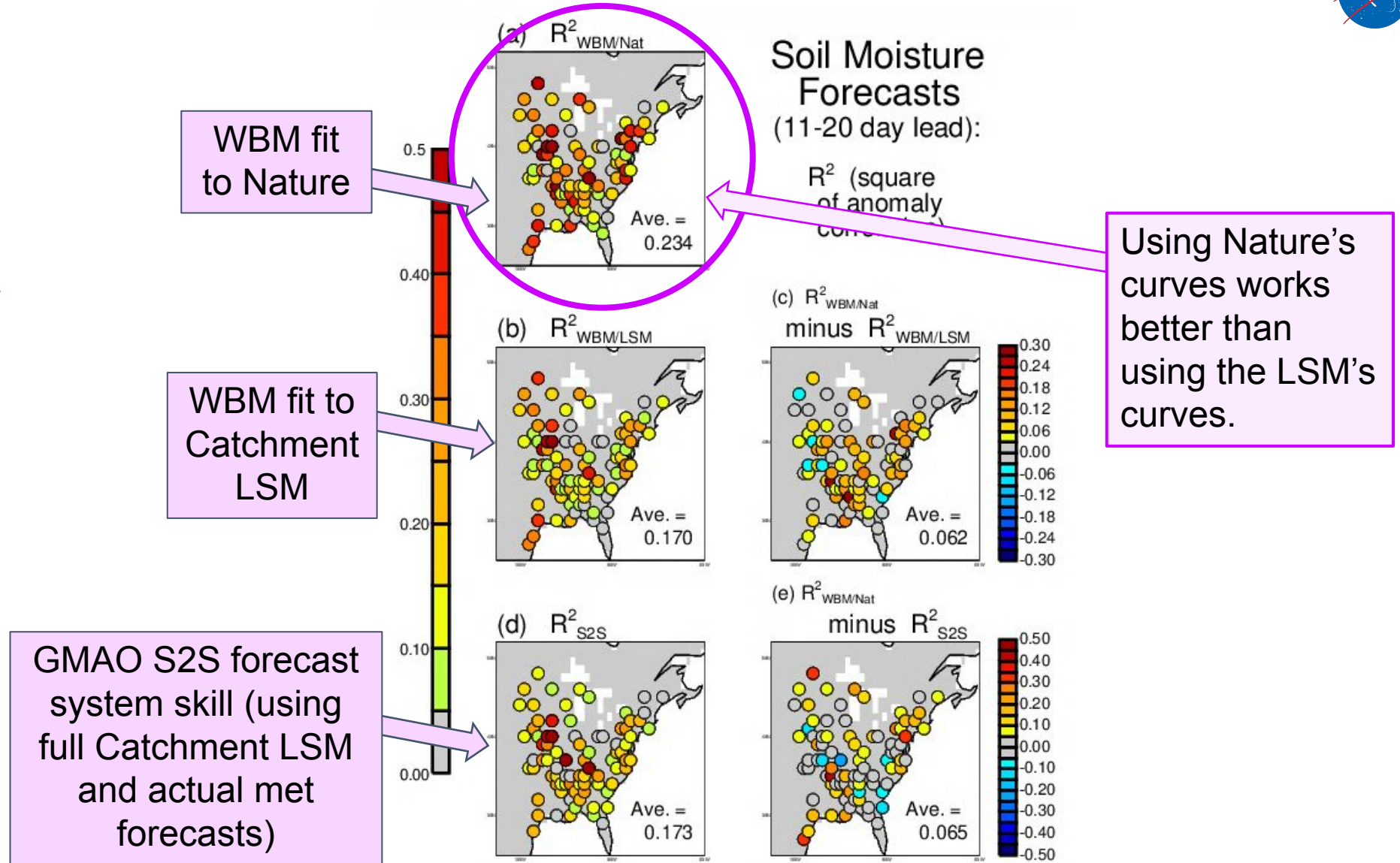


Soil Moisture  
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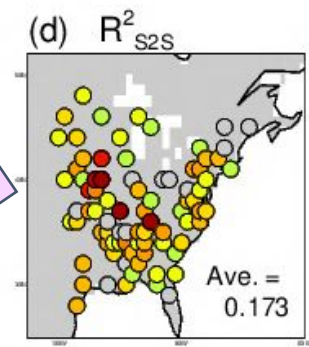
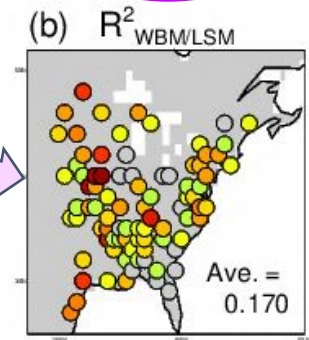
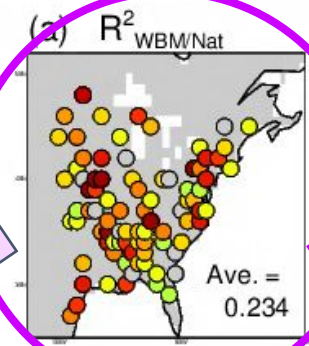
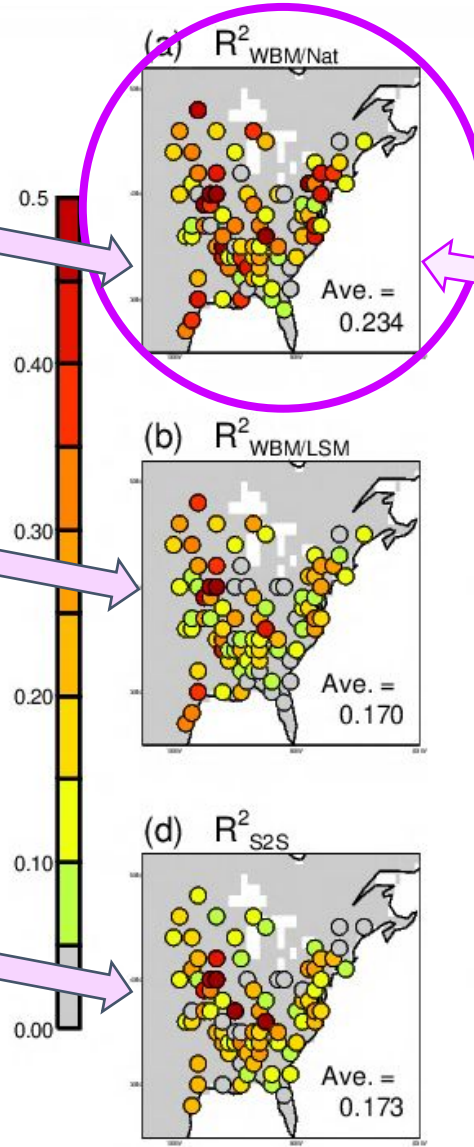
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**Results for  
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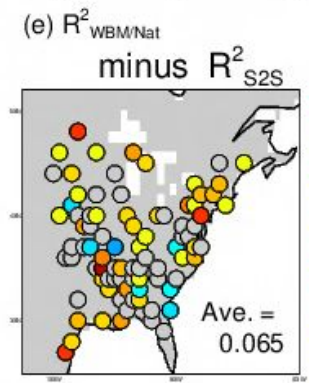
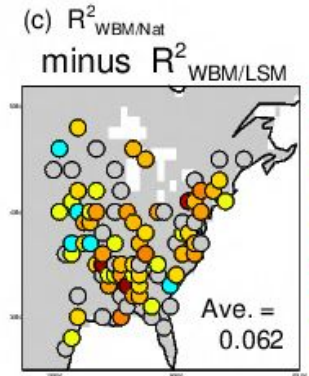
GMAO S2S forecast  
system skill (using  
full Catchment LSM  
and actual met  
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WBM fit  
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WBM fit to  
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LSM



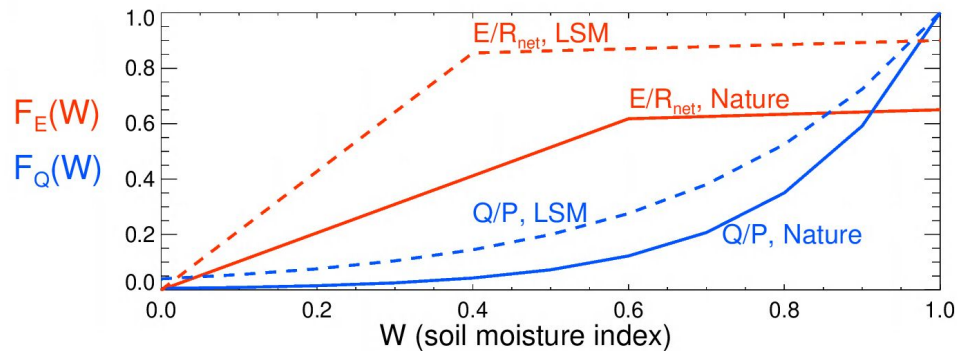
Soil Moisture  
Forecasts  
(11-20 day lead):  
 $R^2$  (square  
of anomaly  
coeff.)



Using Nature's  
curves works  
better than  
using the LSM's  
curves.

## Implications of all this:

- As illustrated here and in past work, an LSM's implicit  $E/R_{net}$  vs.  $W$  and  $Q/P$  vs.  $W$  relationships control, to first order, its hydrological behavior.
- An LSM's relationships may be sub-optimal.



Again, see:

[doi:10.1175/JHM-D-22-0050.1](https://doi.org/10.1175/JHM-D-22-0050.1)

- Calibrating the LSM's parameterizations to bring the relationships more in line with "Nature's curves" should lead to improved performance in subseasonal hydrological forecasting.
- Important side note: the WBM could never replace a full LSM in a complex reanalysis or forecast system given other important roles played by the LSM.







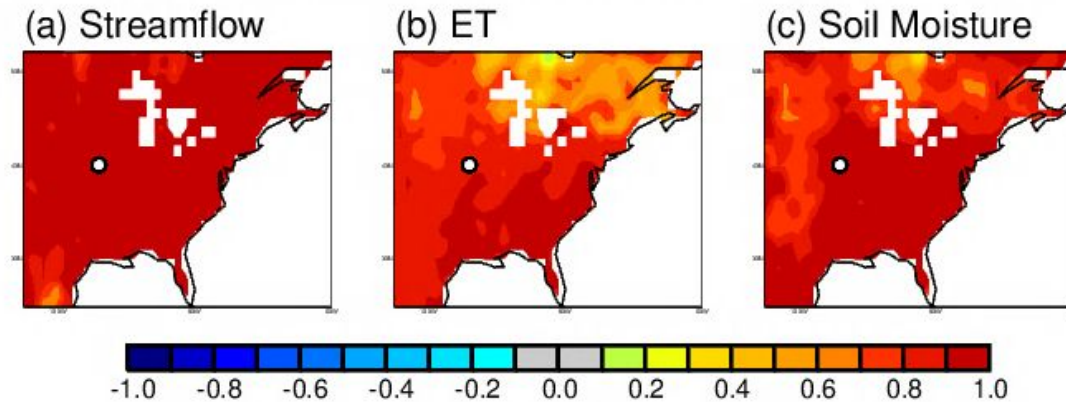




High anomaly correlations between the bare-bones representation (the “WBM”) and the full Catchment LSM as used in MERRA-2



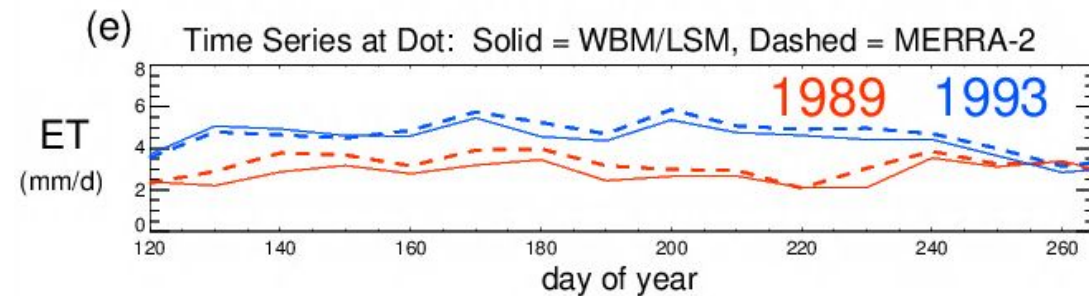
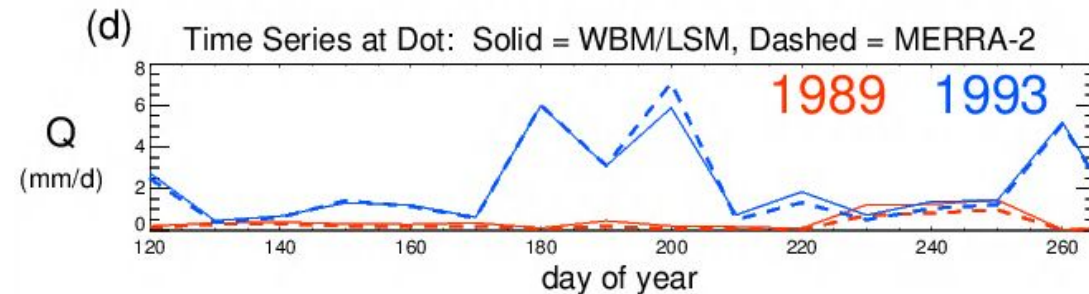
## Anomaly Correlation: WBM/LSM vs. MERRA-2

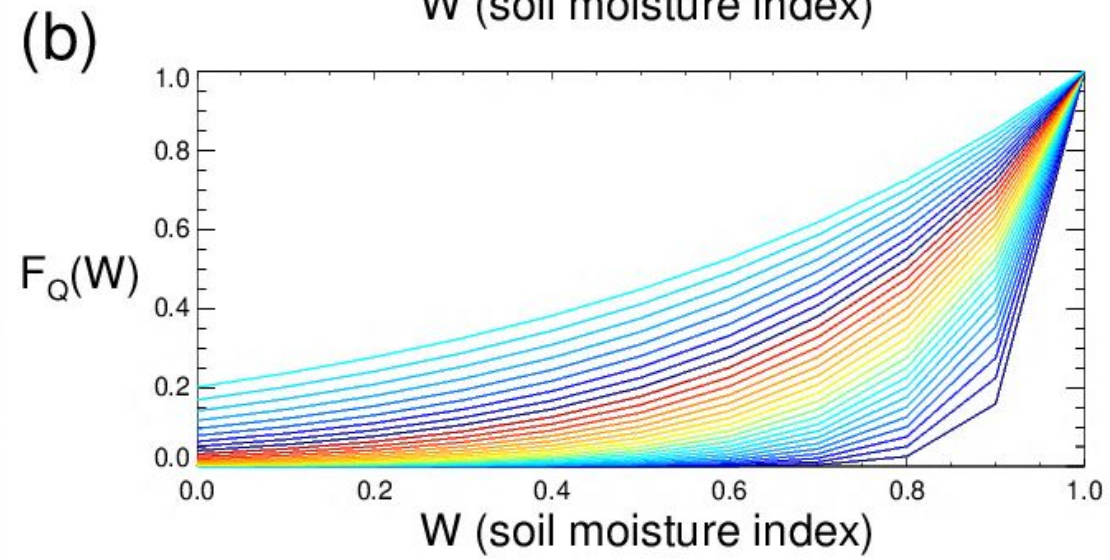
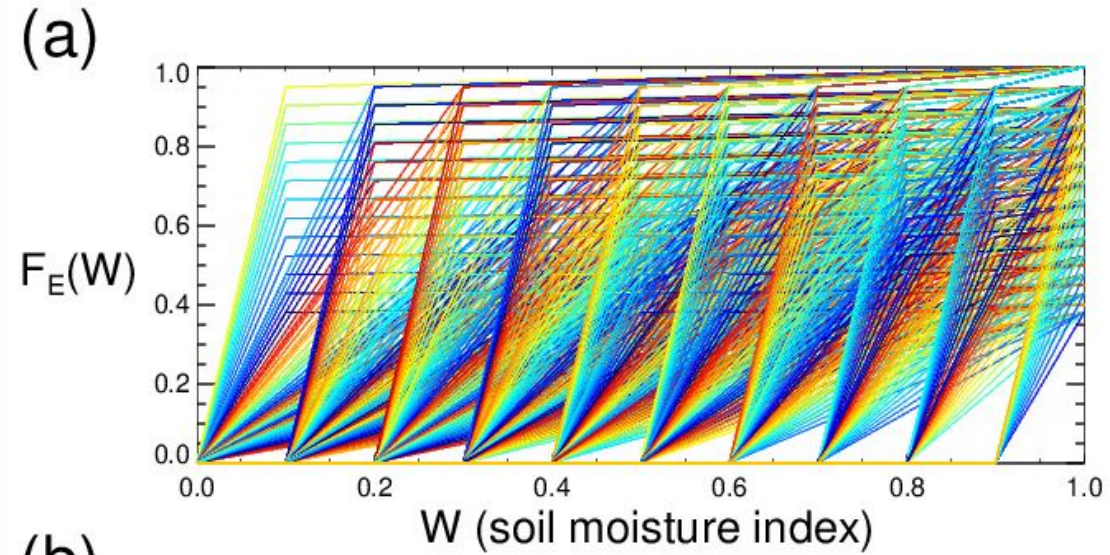


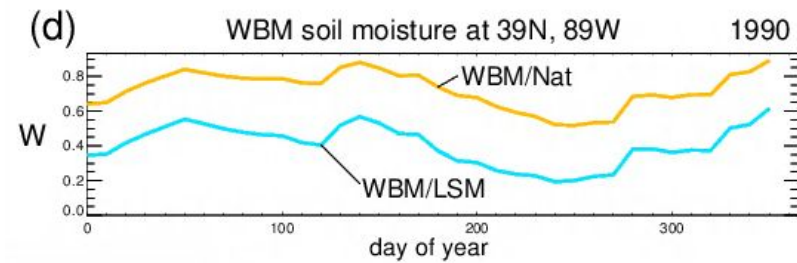
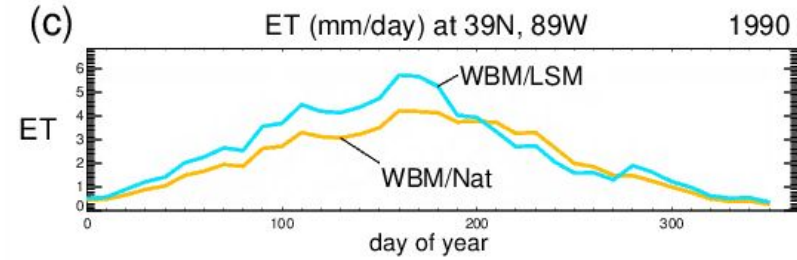
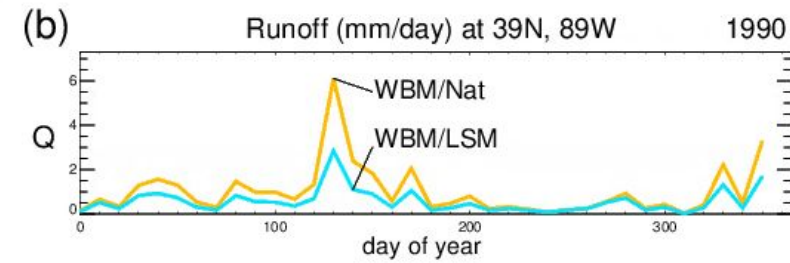
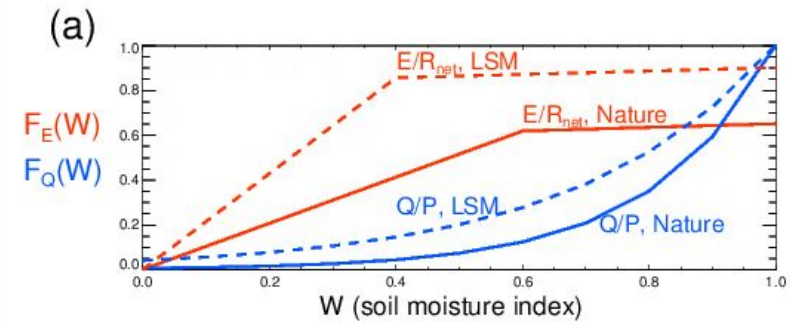
Sample time series comparisons



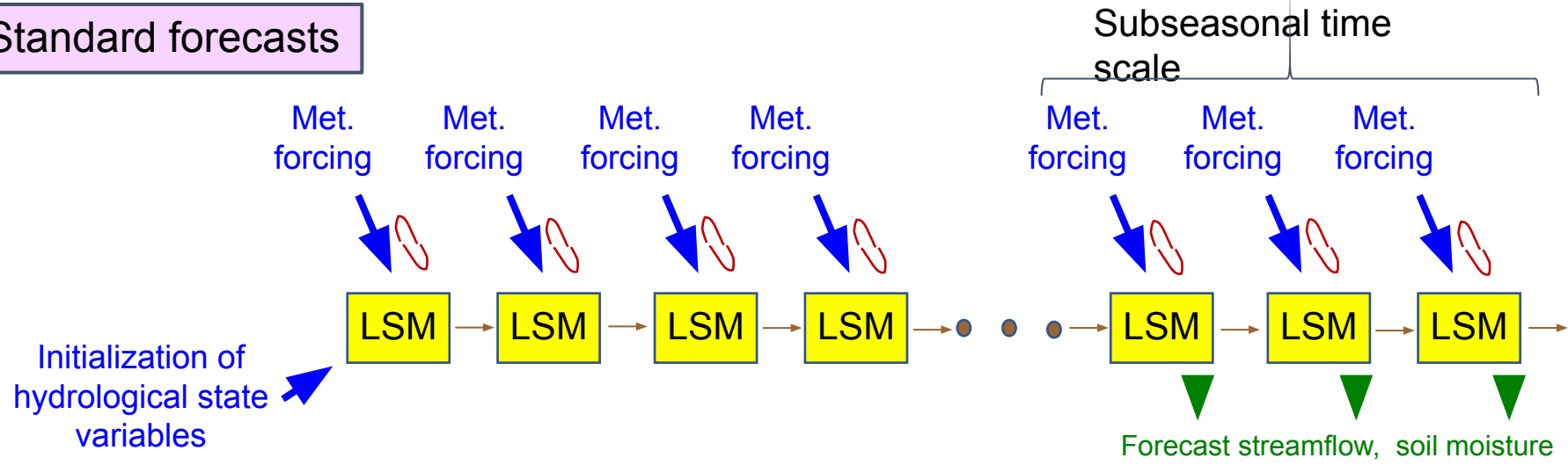
*The bare-bones representation does capture the hydrological behavior of the full LSM!*



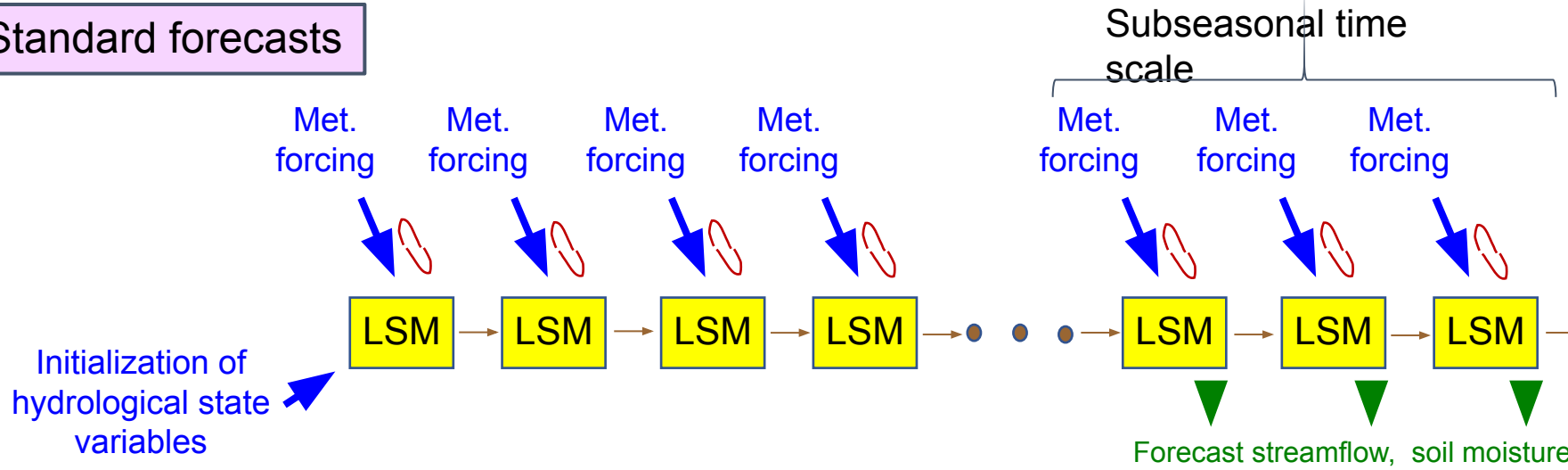




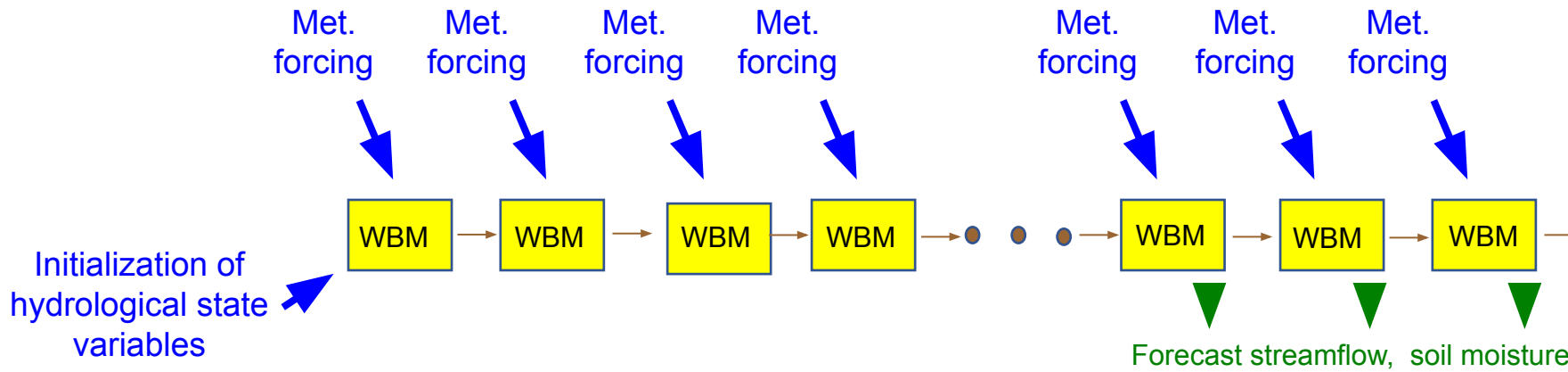
# Standard forecasts



## Standard forecasts



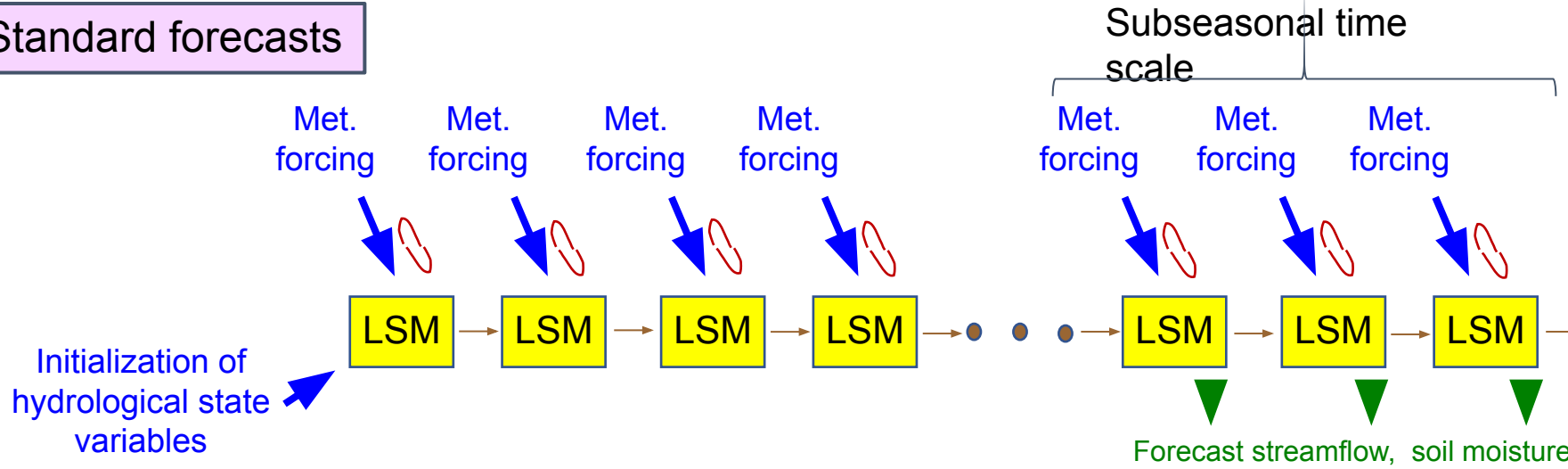
## Offline forecasts using bare-bones (WBM) representation



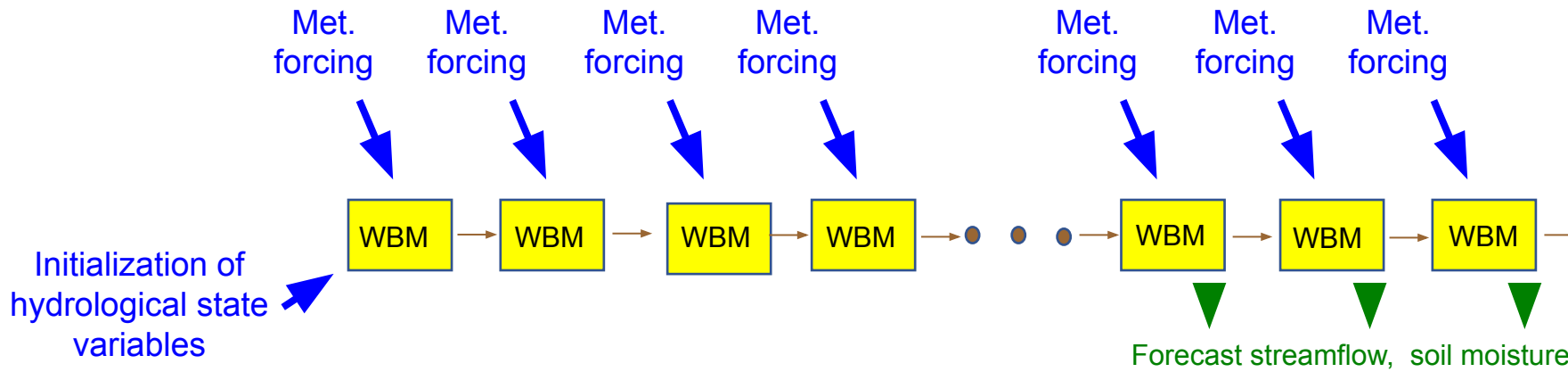
Let WBM represent Catchment LSM



### Standard forecasts



### Offline forecasts using bare-bones (WBM) representation



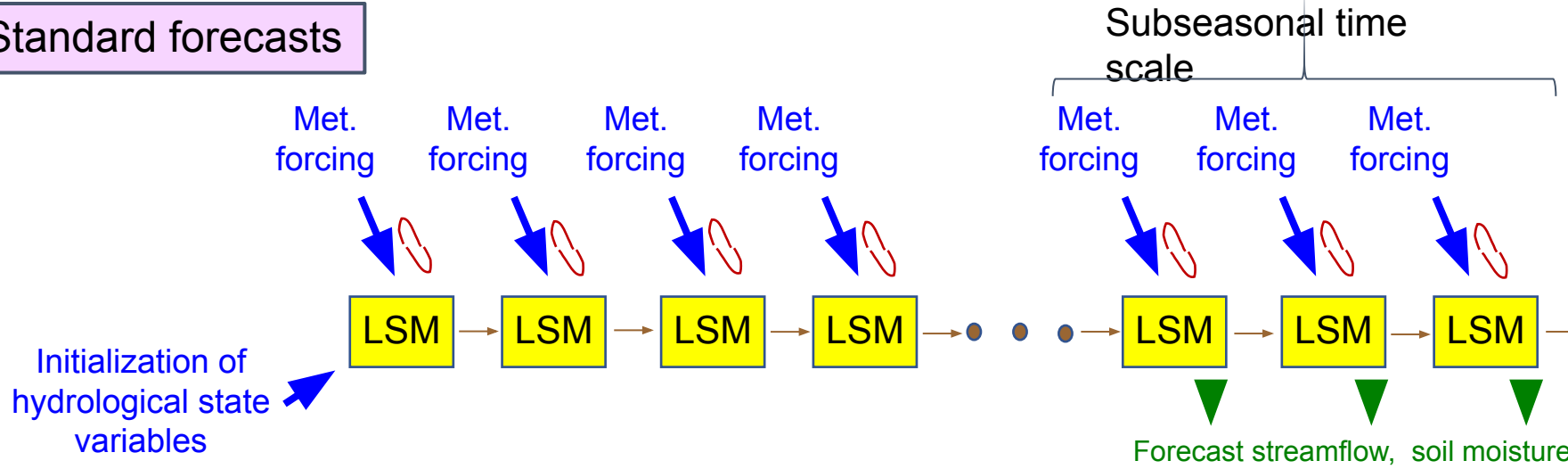
*If met forecast is the same, hydrological forecast skill should be similar*

Let WBM represent Catchment LSM

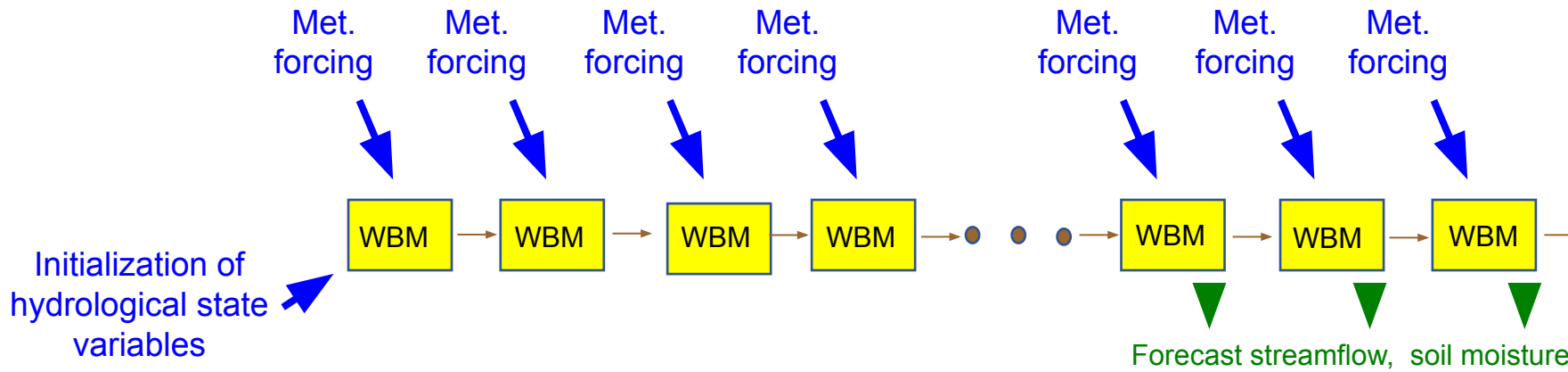




## Standard forecasts



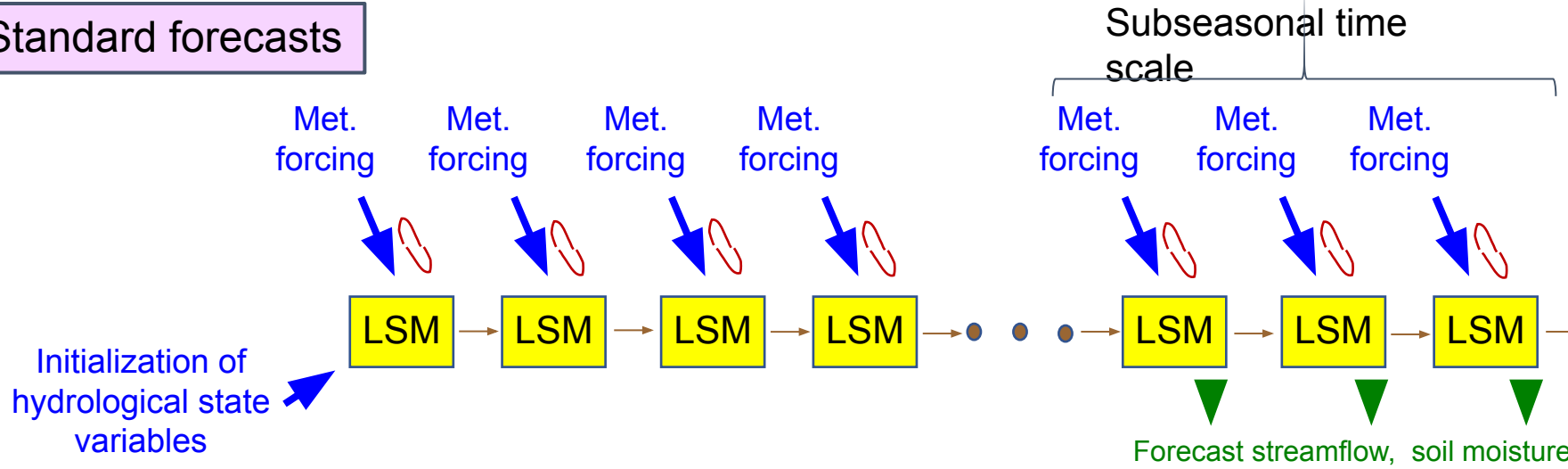
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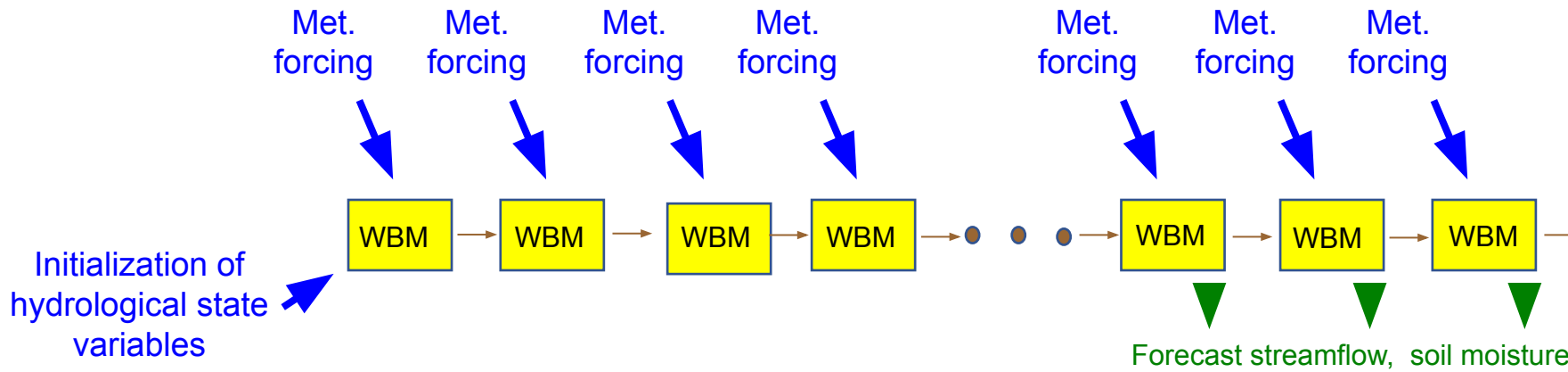
Let WBM represent what happens in Nature



### Standard forecasts



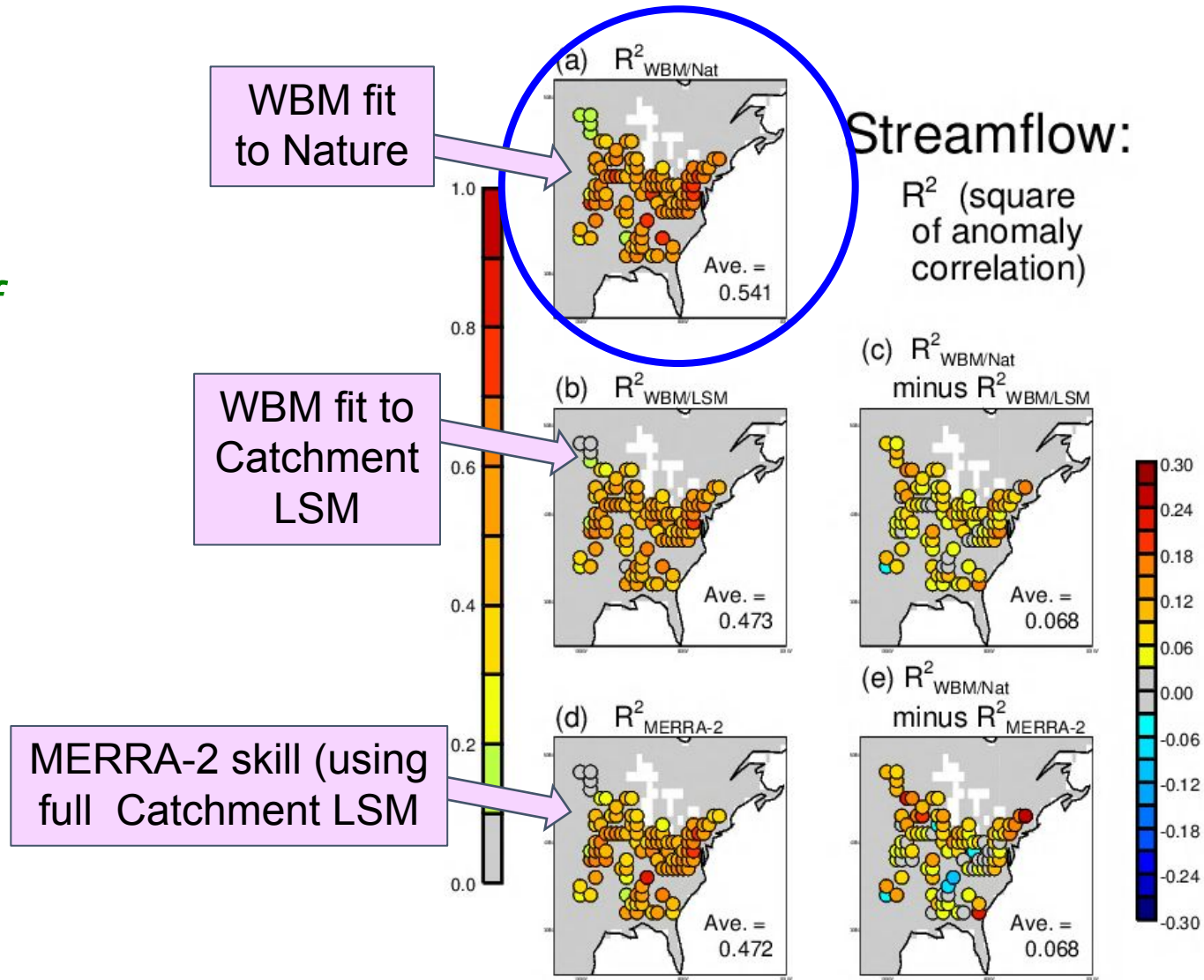
### Offline forecasts using bare-bones (WBM) representation



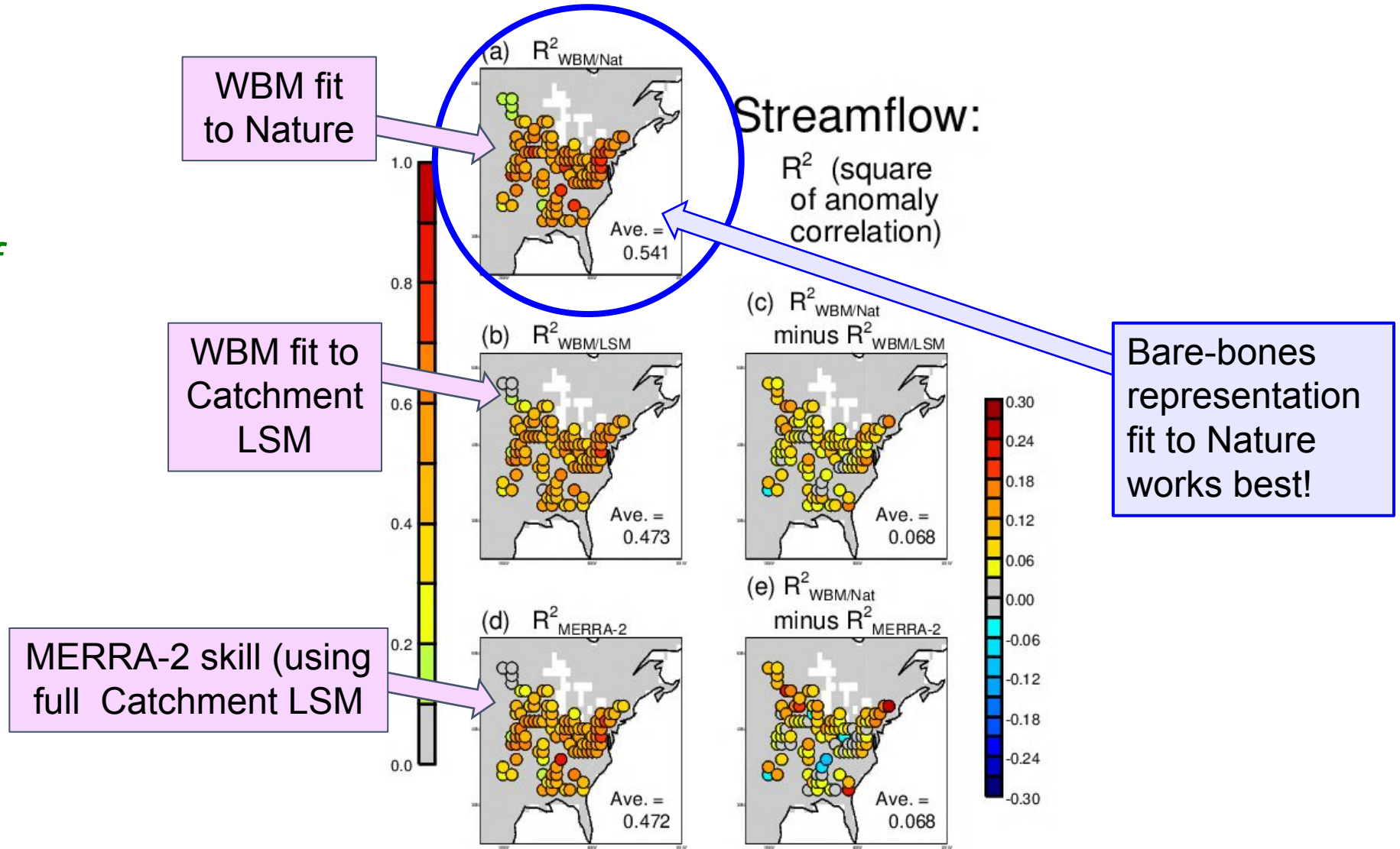
*Again, hypothesize: If met forecast is the same, the hydrological forecast skill here should be higher*

Let WBM represent what happens in Nature

*Skill ( $R^2$  vs obs.)  
assuming “perfect”  
meteorological  
forecasts –  
basically, the skill of  
a hydrological  
simulation with  
observed forcing*



*Skill ( $R^2$  vs obs.)  
assuming “perfect”  
meteorological  
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basically, the skill of  
a hydrological  
simulation with  
observed forcing*



*Skill ( $R^2$  vs obs.)  
assuming zero-skill  
meteorological  
forecasts*

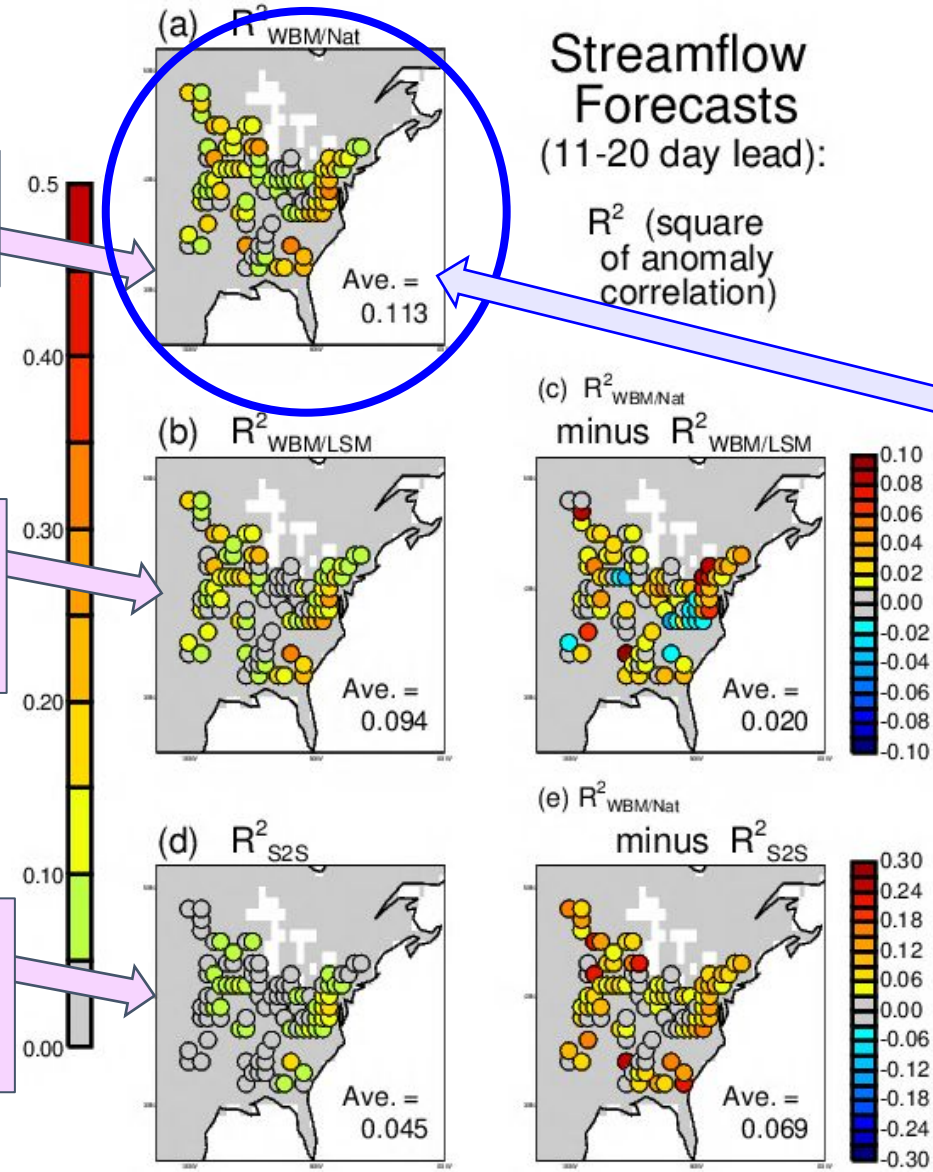
Streamflow  
Forecasts  
(11-20 day lead):

$R^2$  (square  
of anomaly  
correlation)

WBM fit  
to Nature

WBM fit to  
Catchment  
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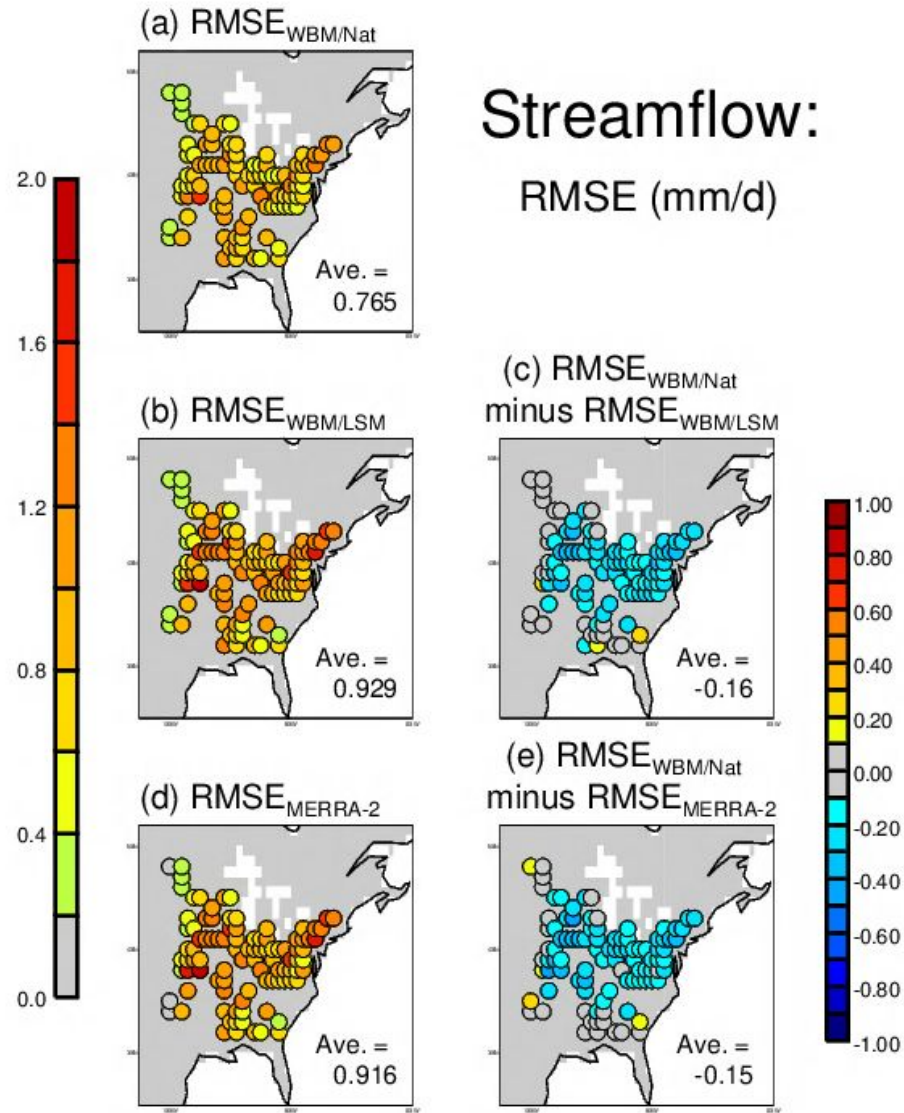
GMAO S2S forecast  
system skill (using  
full Catchment LSM



The bare-bones  
representation  
fit to Nature  
again works  
best!

# Streamflow:

RMSE (mm/d)



# Streamflow:

Bias (mm/d)

